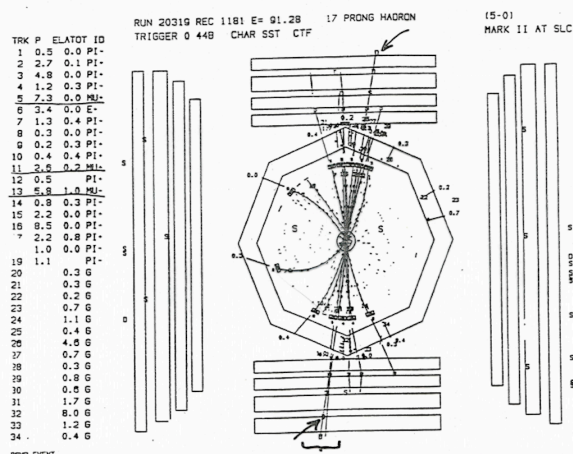


Muons, muon detectors, and muon detectors I have known

With 2 muons

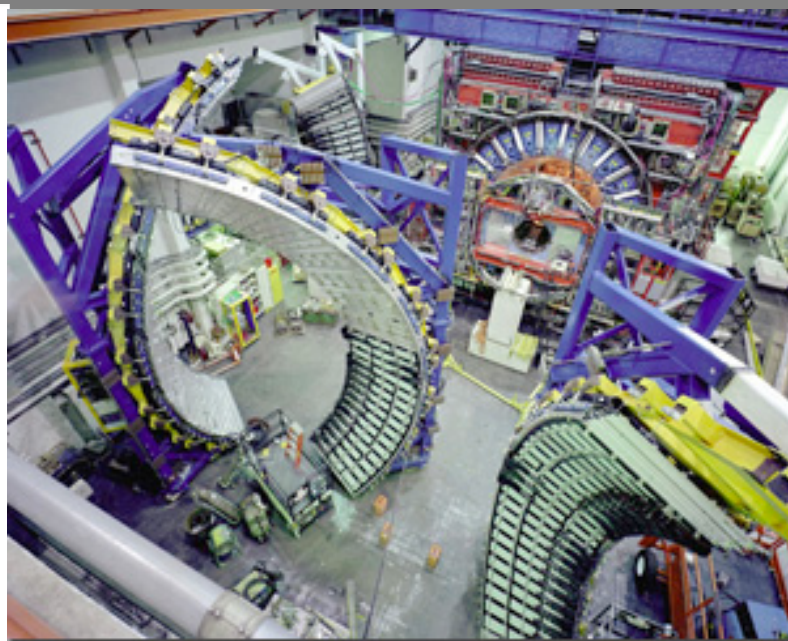


MUON CANDIDATES:

Track 5 $P = 7.3 \text{ GeV}/c$ $P_t = 0.8 \text{ GeV}/c$

Track 13 $P = 5.8 \text{ GeV}/c$ $P_t = 1.0 \text{ GeV}/c$

MarkII at SPEAR



CDF



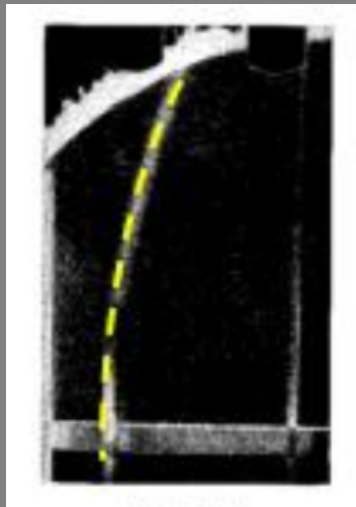
ATLAS

ATLAS NSW

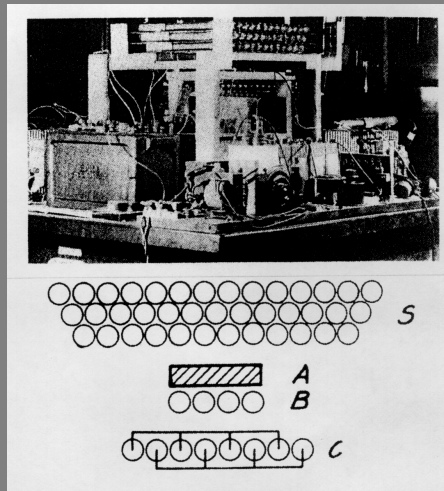


MUON DISCOVERY

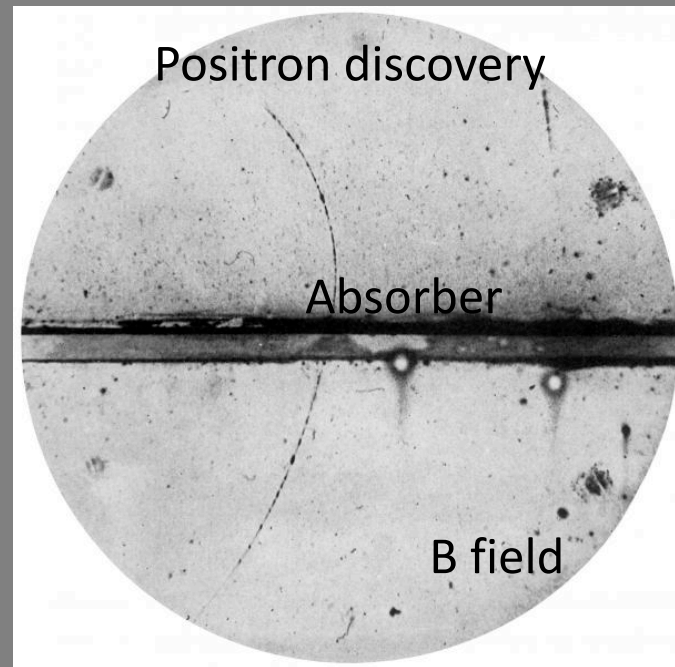
1937 Cloud chamber -
Anderson & Neddermeyer,
Street & Stevenson



Muon candidate track



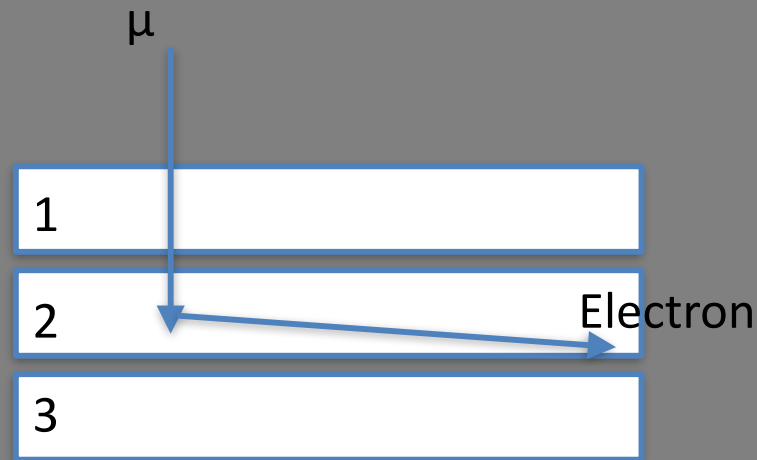
Cosmic ray detector



Same as it ever was: Use cloud chamber as precision tracking and geiger tubes as trigger - measure mass using magnetic field and velocity measurement.
 $mass = qBr/v$. Muon has mass between proton and electron, & doesn't shower and doesn't seem to have strong interactions.

Muon Lifetime

Rossi & Hall 1941



Muon stops, then decays to an electron etc
scintillators: require 1.2 and .not.3



Time Dilation demonstration video

<https://www.youtube.com/watch?v=rbzt8gDSYIM>

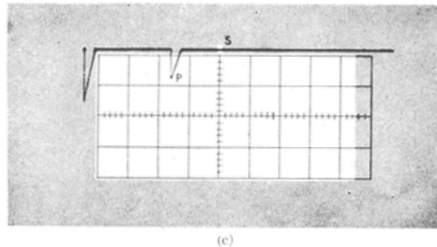
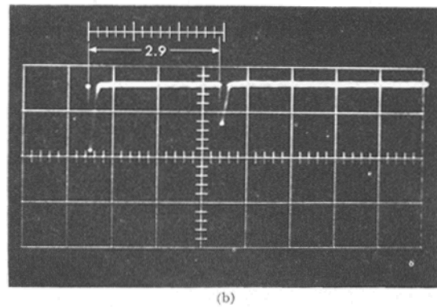
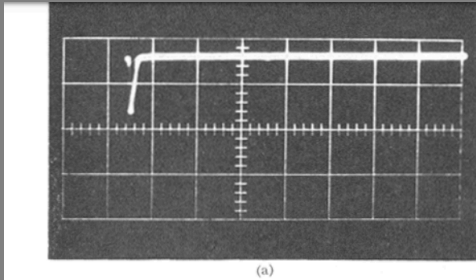


FIG. 4. (a) This photograph shows a single trace caused by a μ -meson traversing the scintillator. Each major division of the time scale is one μ sec. (b) This photograph shows a single trace caused by a μ -meson stopping in the scintillator and decaying after 2.9μ sec. The ionization caused by the resultant electron produces the second pulse. (c) The drawing shows the position which the events recorded in (b) would have had during the experiment. The undeflected oscilloscope traces were behind the mask (shaded area) during the experiment. Only pulses (like P) from the decay electrons were visible. The small slit (S) in the mask was used to position the oscilloscope trace. A total sweep length of 8.5μ sec was used to detect the decay pulses.

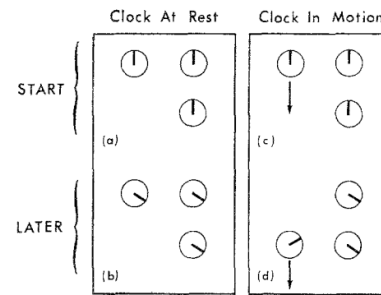


FIG. 1. The behavior of a moving clock. (a) Clocks at rest at time of synchronization; (b) clocks after remaining at rest until a later time; (c) one clock in motion at time of synchronization; (d) the same clock in motion at a later time. Note that the elapsed time read in Fig. 1(d) would be the same even if the moving clocks were started suddenly into motion from rest just after the time of synchronization, and then stopped suddenly just before the time of later observation. The elapsed time as read by the observer depends explicitly on only how long it has been in motion and at what speed relative to the observer, not on its initial or final state of motion, or on any acceleration that it has undergone.



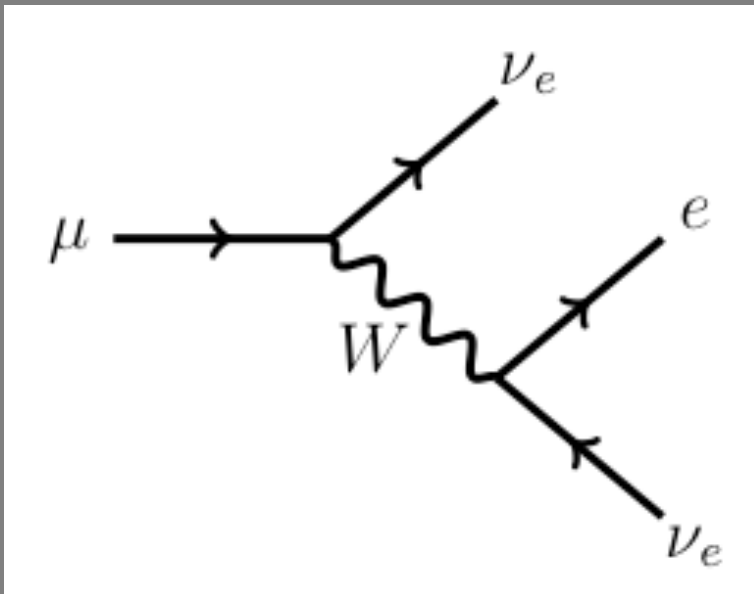
Smith



1963 Frisch and Smith: Time Dilation
The Movie

What we know now

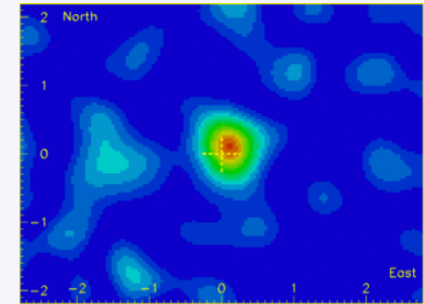
the long lifetime
(2.2microseconds) of the muon
was surprising presaging a new
energy scale - the weak scale.



$$\tau = 1/\Gamma$$

$$\Gamma \propto \frac{m_{\mu}^4}{M_W^4} m_{\mu} c^2$$

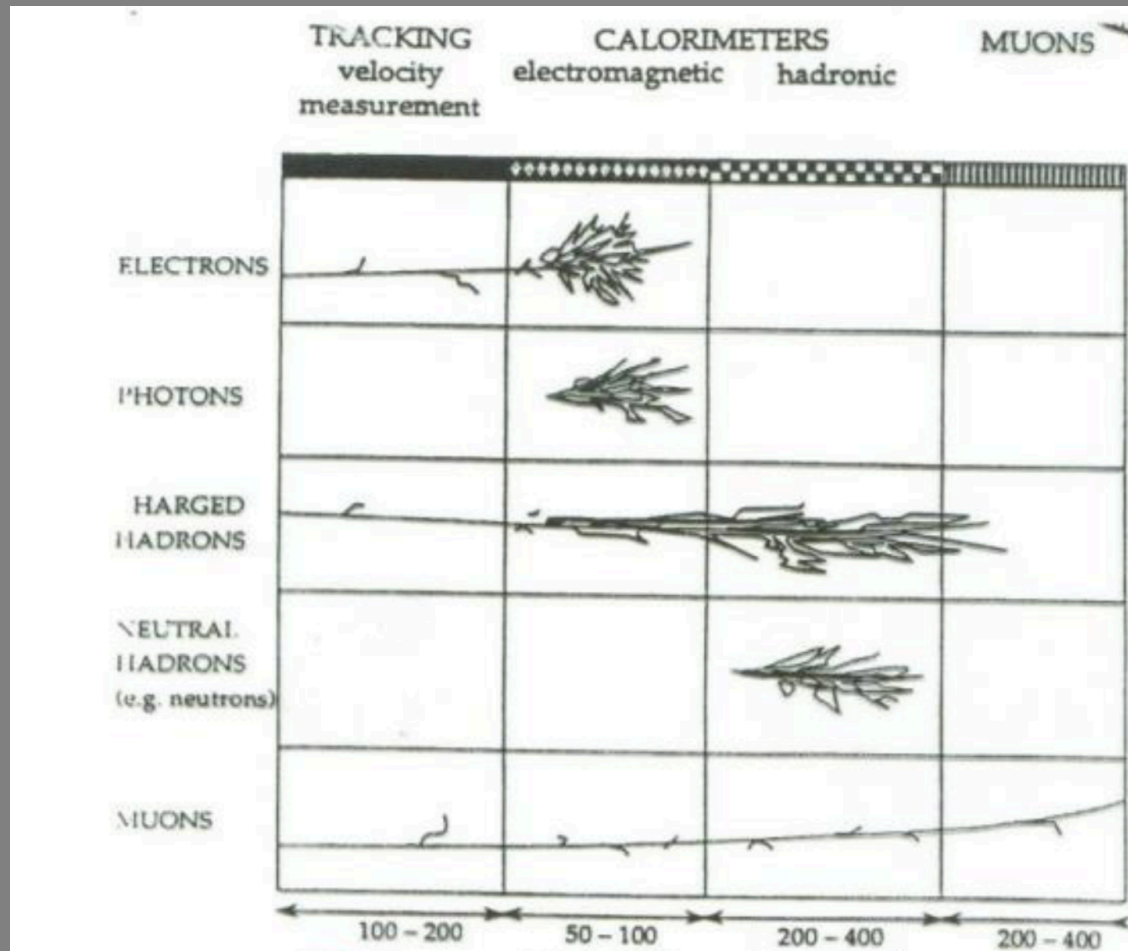
Muon



The Moon's [cosmic ray](#) shadow, as seen in secondary muons generated by cosmic rays in the atmosphere, and detected 700 meters below ground, at the [Soudan II](#) detector

Composition	Elementary particle
Statistics	Fermionic
Generation	Second
Interactions	Gravity, Electromagnetic, Weak
Symbol	μ^-
Antiparticle	Antimuon (μ^+)
Discovered	Carl D. Anderson , Seth Neddermeyer (1936)
Mass	105.658 3755(23) MeV/c² ^[1] 0.113 428 9259(25) Da ^[1]
Mean lifetime	2.196 9811(22) $\times 10^{-6}$ s ^{[2][3]}
Decays into	e^- , $\bar{\nu}_e$, ν_{μ} ^[3] (most common)
Electric charge	-1 <i>e</i>
Color charge	None
Spin	$\frac{1}{2}$

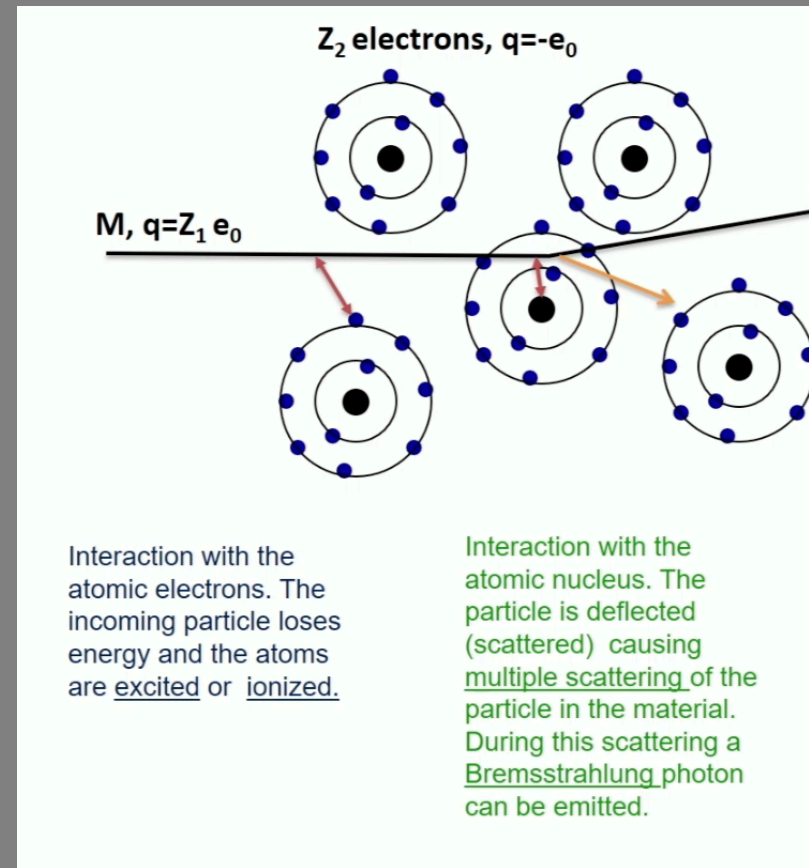
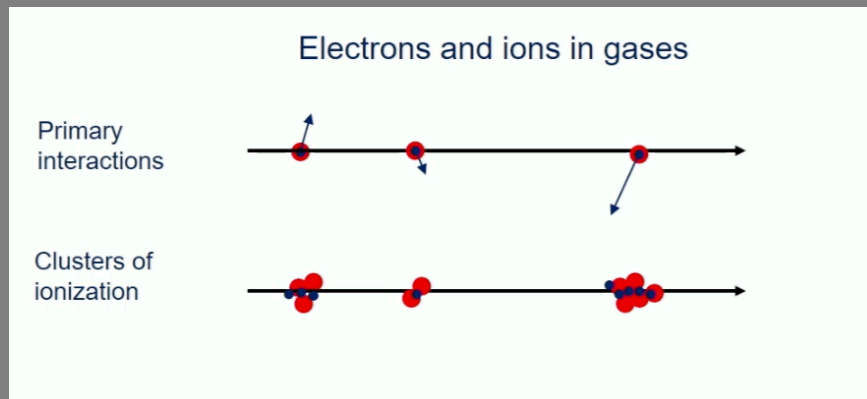
Particle interactions phenomenology



Low ρ . High ρ . High ρ . ?

How does the muon interact in matter

- Muons predominately lose energy through ionization

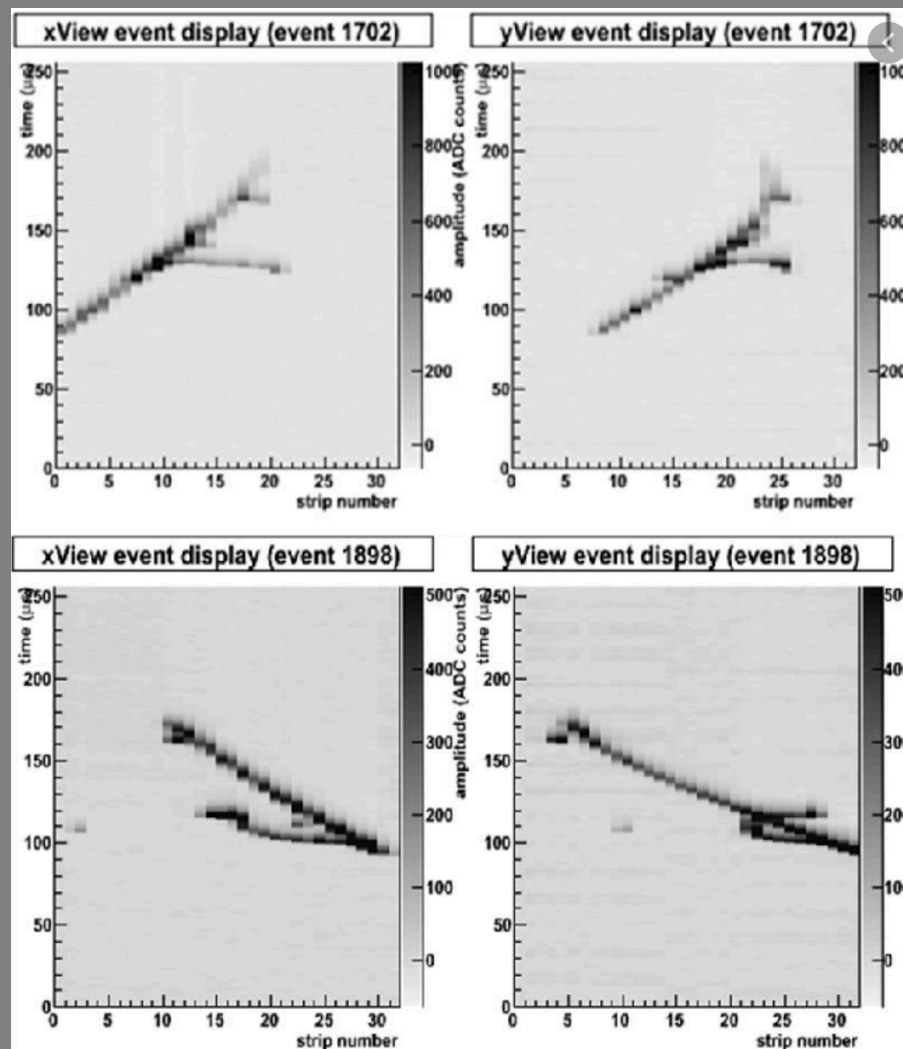


From talk by Werner Riegler - CERN summer school

Delta Rays

Sometimes the electrons that have been ionized have enough energy to ionize again

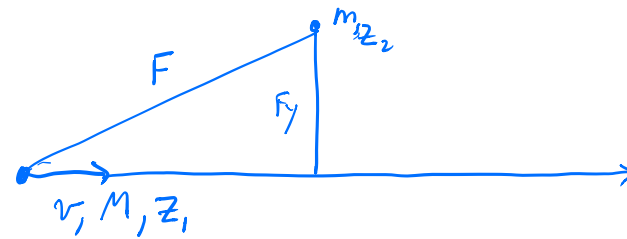
This can make tracking more difficult



Two views of 2 muons with delta rays- TPC

Ionization vs Brehmstraalung?

Easier to impart energy to the electrons



$$F_y \rightarrow \Delta p = \int_{-\infty}^{\infty} F_y(t) dt$$

$$\text{Transferred energy } \Delta E = \frac{(\Delta p)^2}{2m} \propto \frac{Z_1^2 Z_2^2}{2m}$$

$$\frac{\Delta E_{\text{electrons}}}{\Delta E_{\text{nucleus}}} \sim \frac{2m_{\text{proton}}}{m_e} \sim 4,000$$

The incoming particle transfers most of its energy to the electrons!

Bethe- Bloch quantum mechanical expression for ionization energy loss by a charged particle

$$-\frac{dE}{dx} = 2\pi N_a r_e^2 m_e c^2 \rho \frac{Z}{A} \frac{z^2}{\beta^2} \left[\ln \left(\frac{2m_e \gamma^2 v^2 W_{\max}}{I^2} \right) - 2\beta^2 - \delta - 2 \frac{C}{Z} \right],$$

with

$$2\pi N_a r_e^2 m_e c^2 = 0.1535 \text{ MeVcm}^2/\text{g}$$

r_e : classical electron
radius = $2.817 \times 10^{-13} \text{ cm}$

m_e : electron mass

N_a : Avogadro's
number = $6.022 \times 10^{23} \text{ mol}^{-1}$

I : mean excitation potential

Z : atomic number of absorbing
material

A : atomic weight of absorbing material

ρ : density of absorbing material
 z : charge of incident particle in
units of e

$\beta = v/c$ of the incident particle

$\gamma = 1/\sqrt{1-\beta^2}$

δ : density correction

C : shell correction

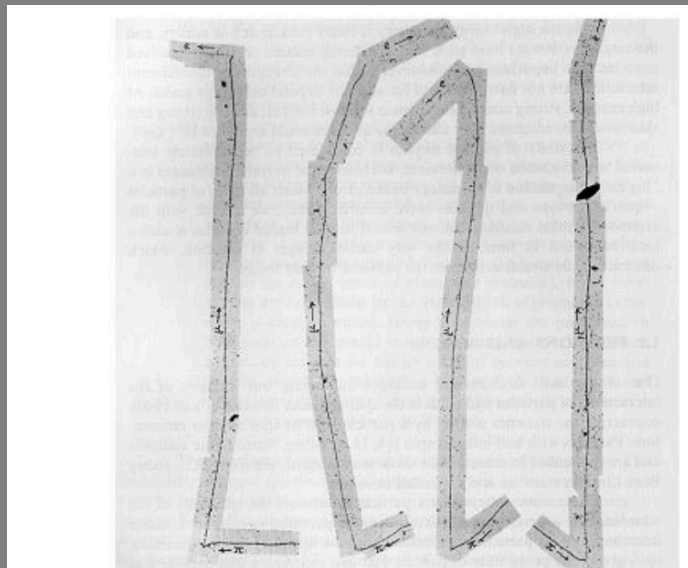
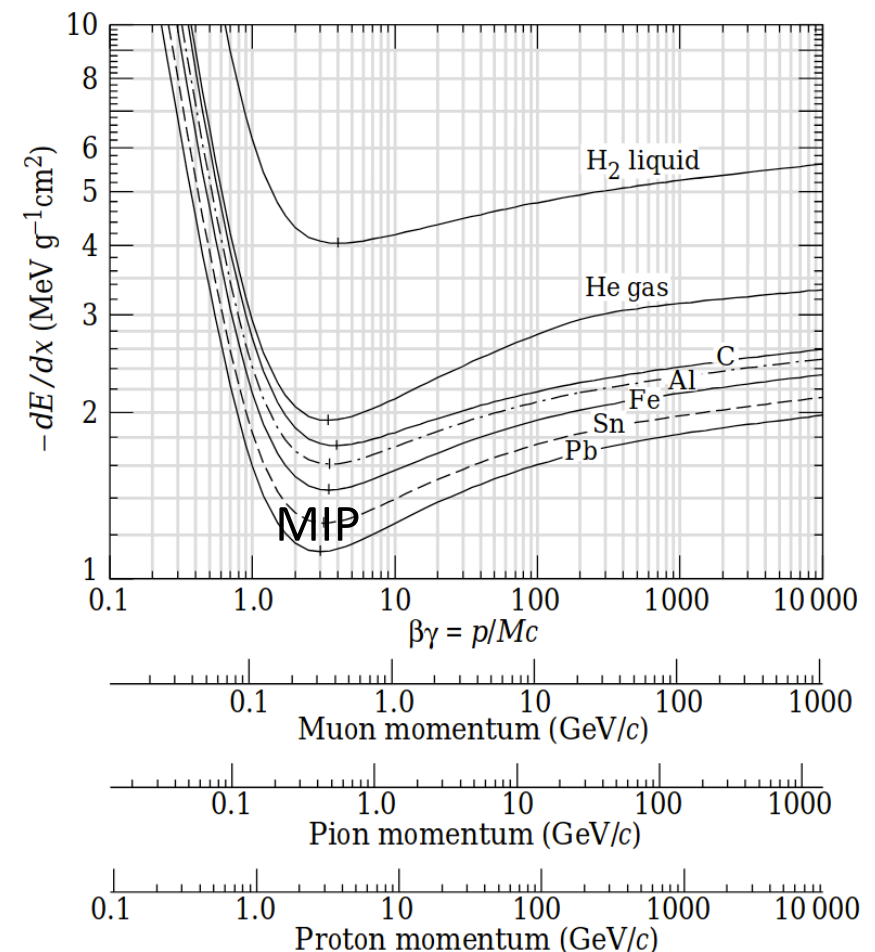
W_{\max} : maximum energy transfer in a
single collision.

$$-\frac{dE}{dx} = 2\pi N_a r_e^2 m_e c^2 \rho \frac{Z}{A} \frac{z^2}{\beta^2} \left[\ln \left(\frac{2m_e \gamma^2 v^2 W_{\max}}{I^2} \right) - 2\beta^2 - \delta - 2 \frac{C}{Z} \right]$$

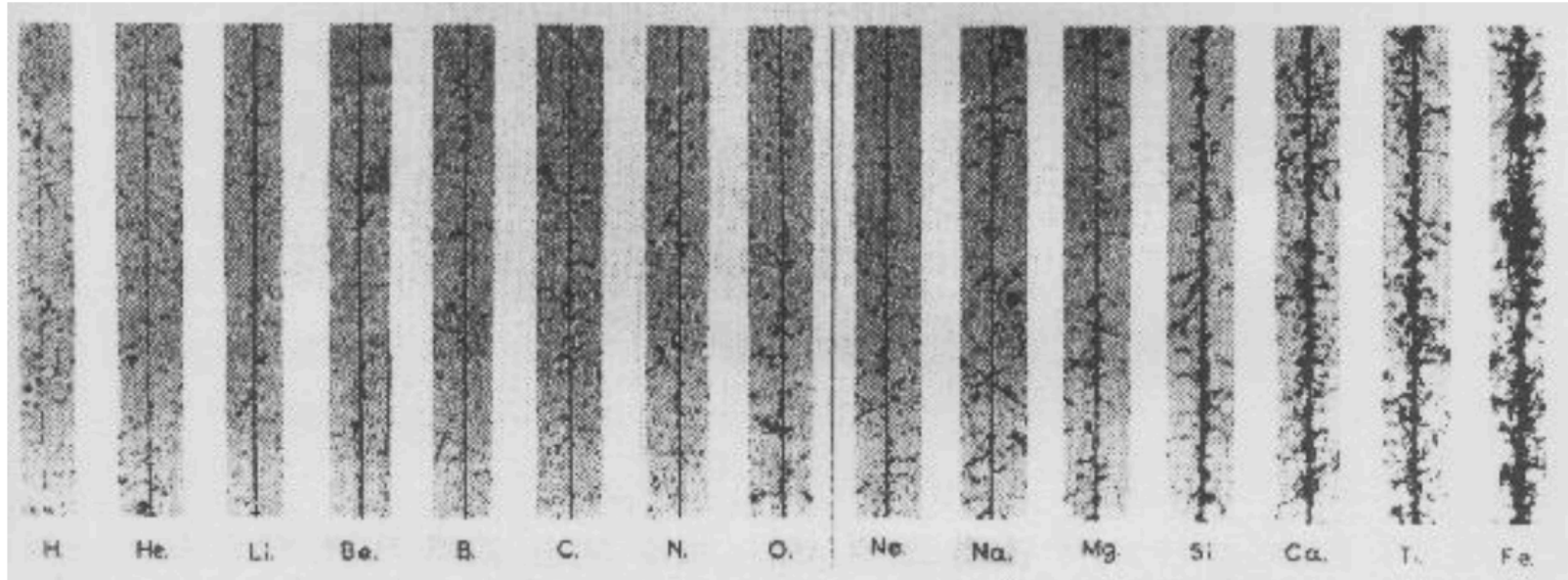
As the velocity goes low
the ionization is high

There is a minimum about 3-3.5 in $\beta\gamma$
This is a Minimum Ionizing particle (MIP)

Really $(1/\rho)dE/dx$



Ionization energy loss depends on the square of the charge on the particle
Traversing the detector.



Z^2 1—4— 9— 16.——————144 -196—————676

Z/A of the material is pretty constant.

Beth Bloch example

Imagine a MIP muon traversing 1 meter of Fe

$Z \sim 0.5A$

From the plot : a MIP ($\beta\gamma \sim 3$) deposits

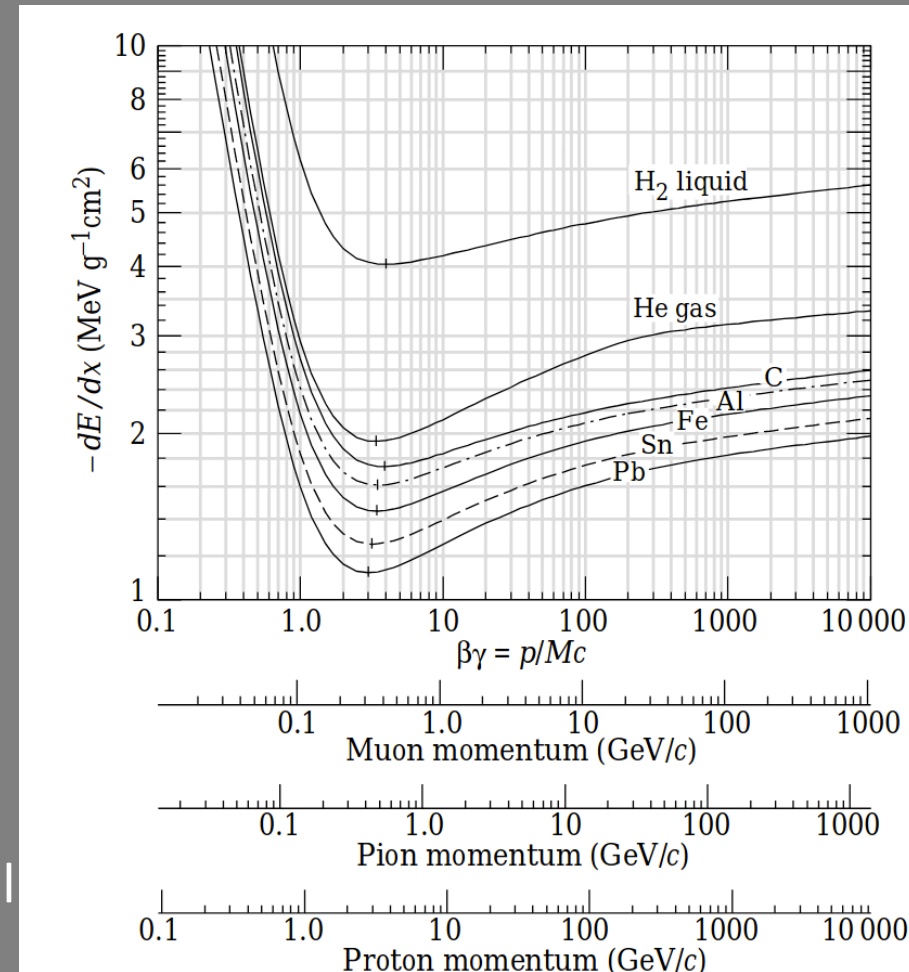
$dE/dx \sim 1.4 \text{ MeV cm}^2/\text{gm}$

But $\rho = 7.87 \text{ g/cm}^3$ so $dE/dx = 11 \text{ MeV/cm}$

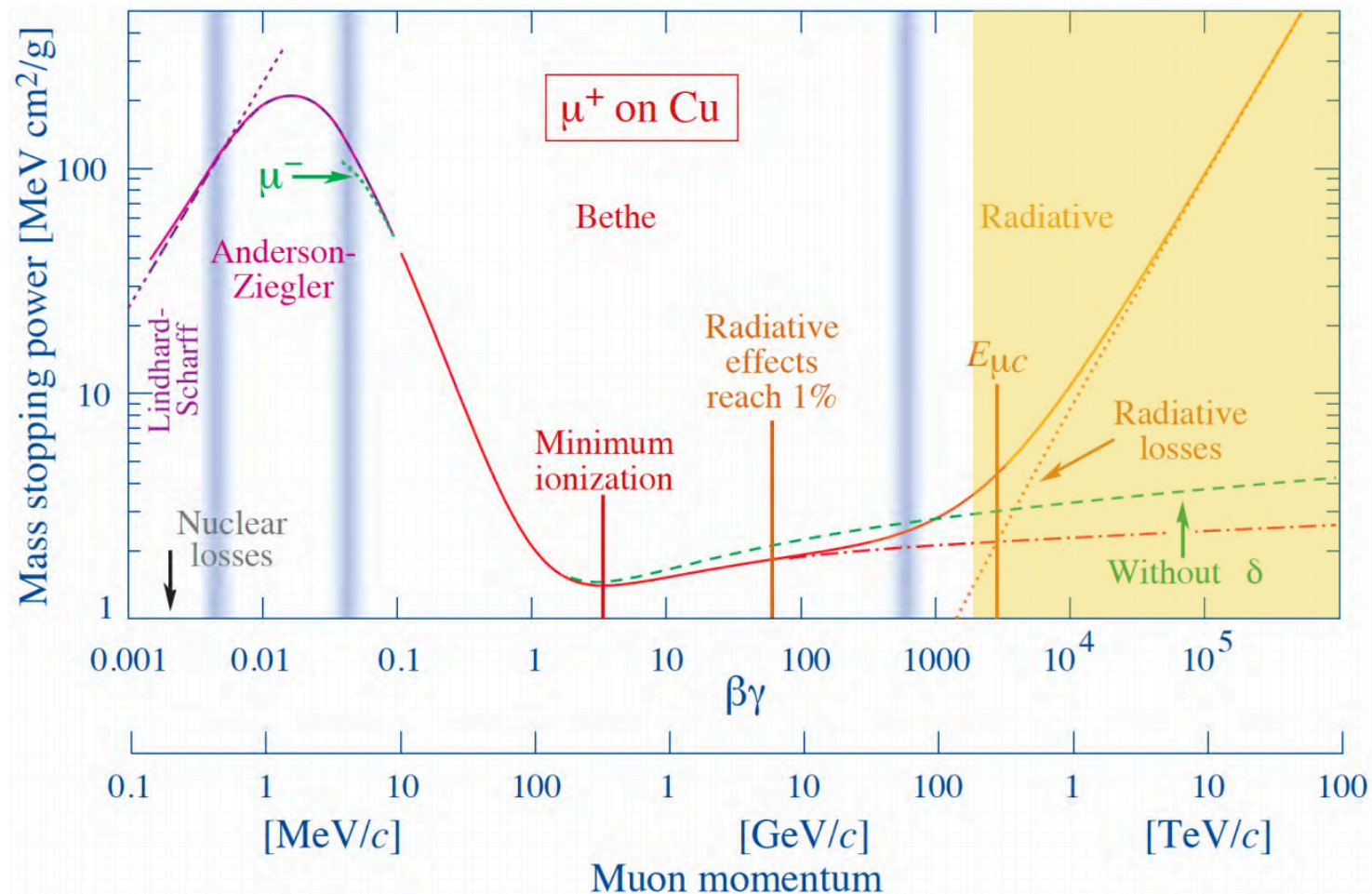
So energy lost over a meter is $dE = 1101 \text{ MeV}$

So a 1 GeV muon can traverse 1 meter of steel
of steel!

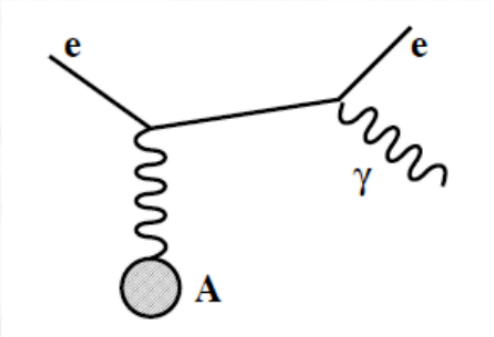
What about a 1 GeV electron or proton?



Bethe Bloch energy loss by ionization - muons on Copper



energy loss by brehmstraalung



$$\left. -\frac{dE}{dx} \right|_{Brems} = 4\alpha N_A \left(\frac{e^2}{mc^2} \right)^2 \ln \frac{183}{Z^{1/3}} \frac{Z(Z+1)}{A} Q^2 E$$

where: Q, m = electric charge and mass of the particle,

α = fine structure constant

A, Z = atomic number, number of protons of the material

N_A = Avogadro's number

So for Brehms: energy loss is proportional to E/m^2

Depends on $Z(Z+1)/A$ and the density of the material

Depends on Q^2 and $1/m^2$ of the incoming particle!

Is linear in E - the energy of the incoming particle

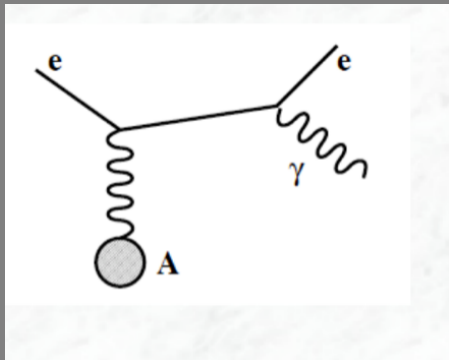
So $(dE_{brehm}/dx)_{muon}/(dE_{brehm}/dx)_{electron} = 1/40,000$

Critical Energy E_c Brehm = ionization

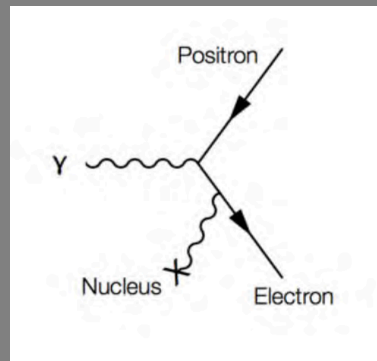
$$-\frac{dE}{dx}\bigg|_{ion}(E_c) = -\frac{dE}{dx}\bigg|_{brems}(E_c)$$

On Cu for instance $Z=29$. $E_c(\text{electrons})=19 \text{ MeV}$ $E_c(\text{muons}) = 1 \text{ TeV}$.

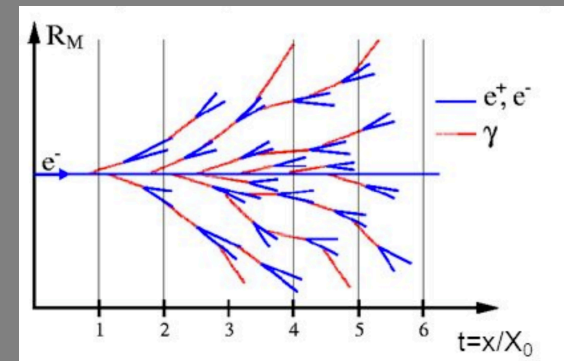
So muons do not shower in material and electrons do!



+



=



Brehm

Pair production

Shower

Plot dE/dx vs $p=Mc\beta\gamma$

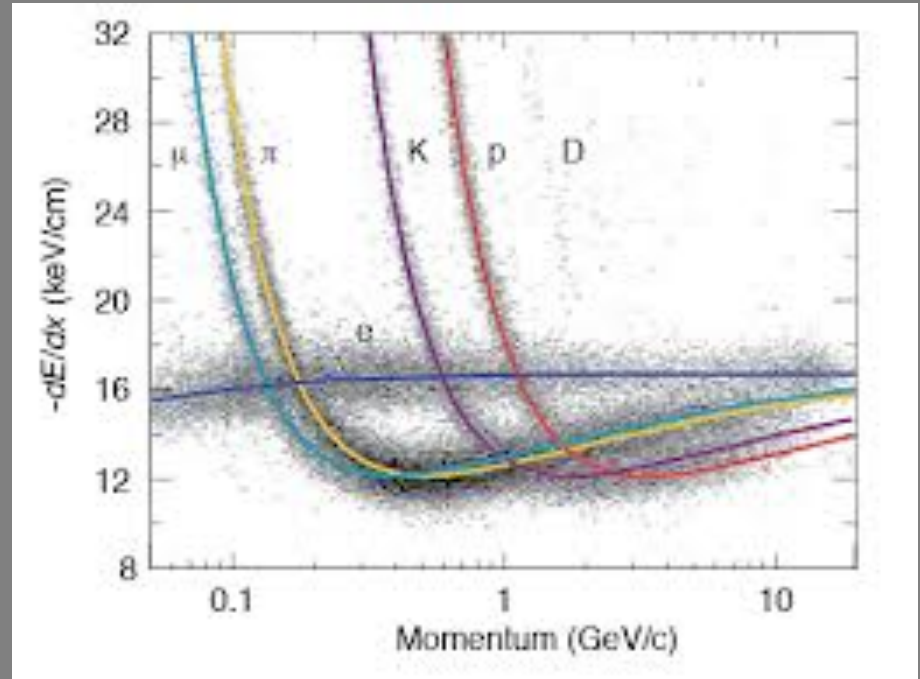
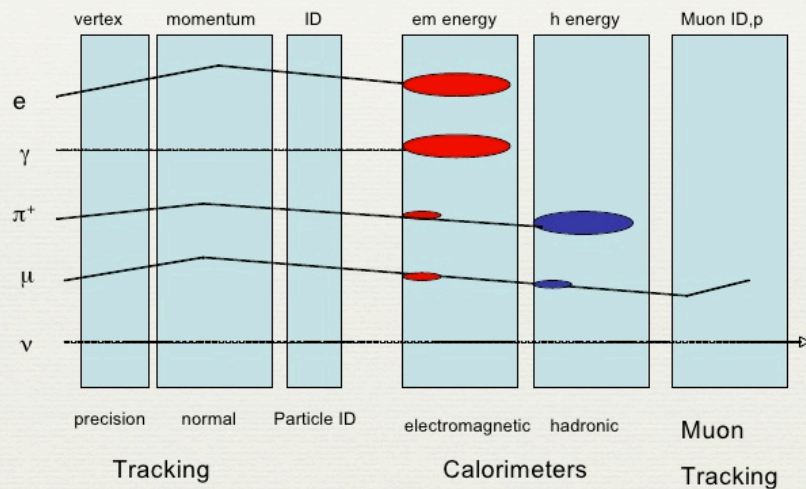
Particle id

Not useful for high p
muons!

$$\beta\gamma = p/mc$$

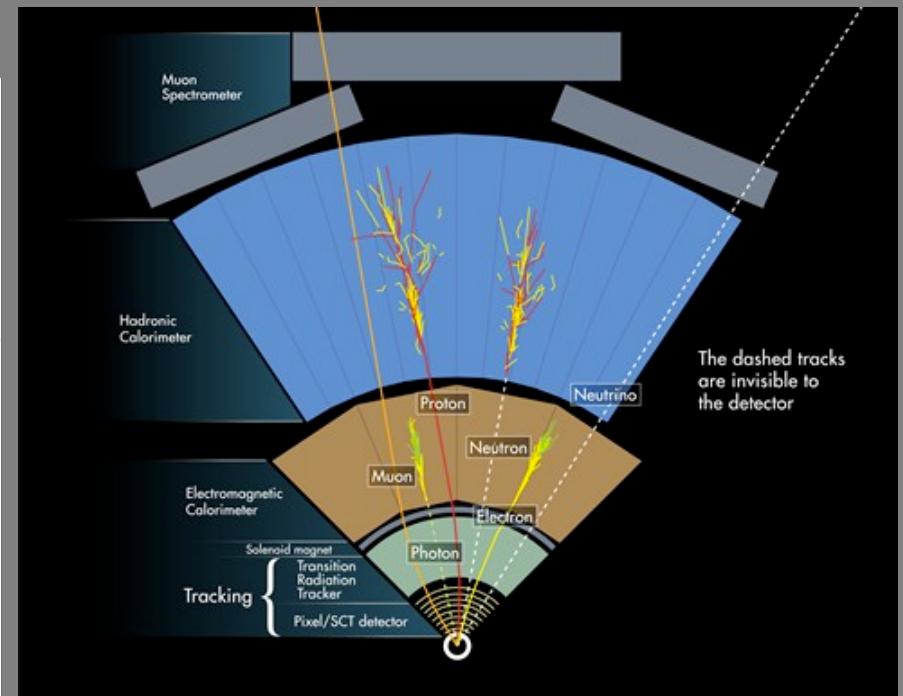
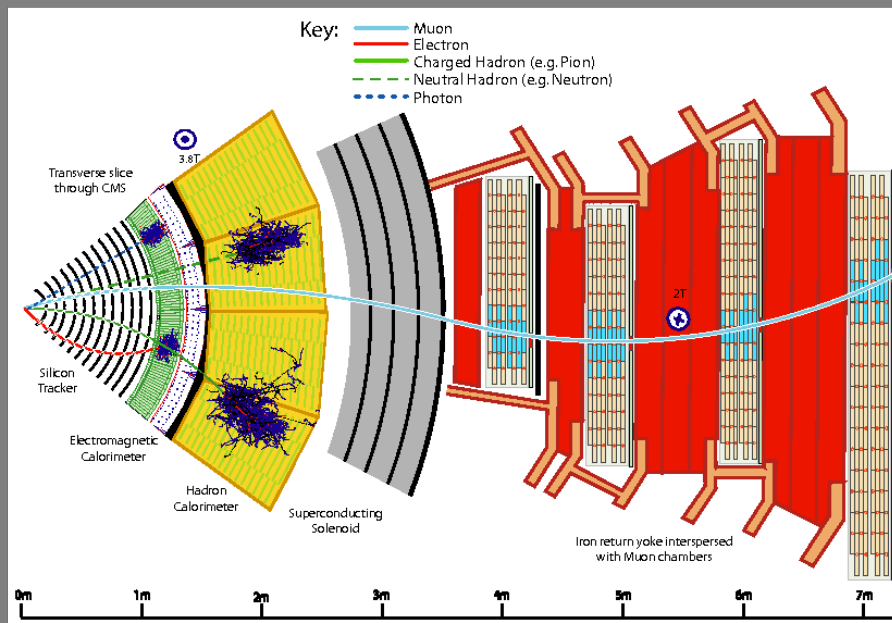
If I know p , and $\beta\gamma$ or dE/dx ,
I know m .

Particle Identification



Measure muon momentum

- Need B fields precision detector, trigger.



Both ATLAS and CMS have an inner detector immersed in a solenoidal field and a Muon spectrometer with a B field - return field of solenoid for CMS - Air core toroid for ATLAS

Flux return:

The combined resolution is best.

Flux return

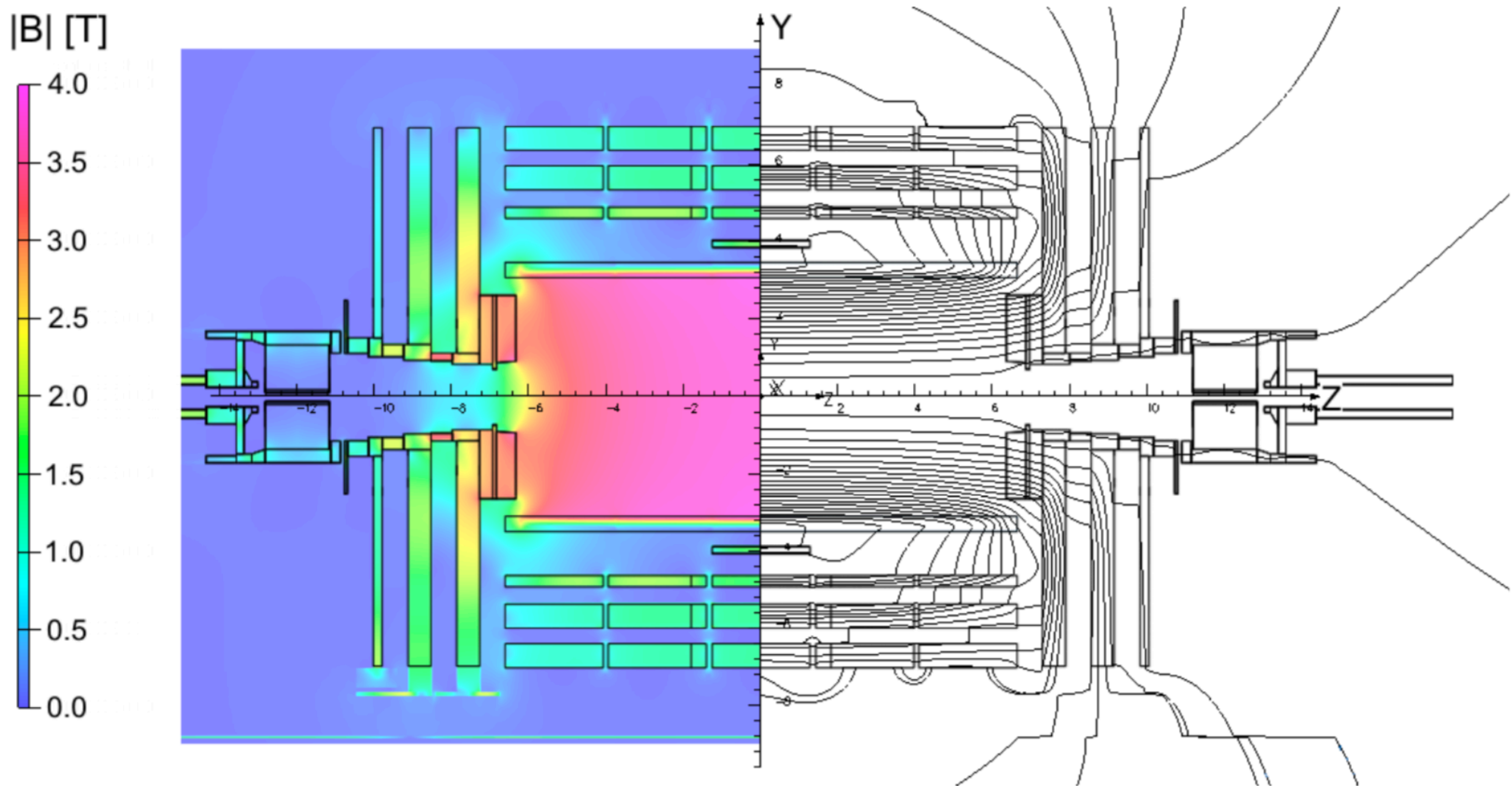
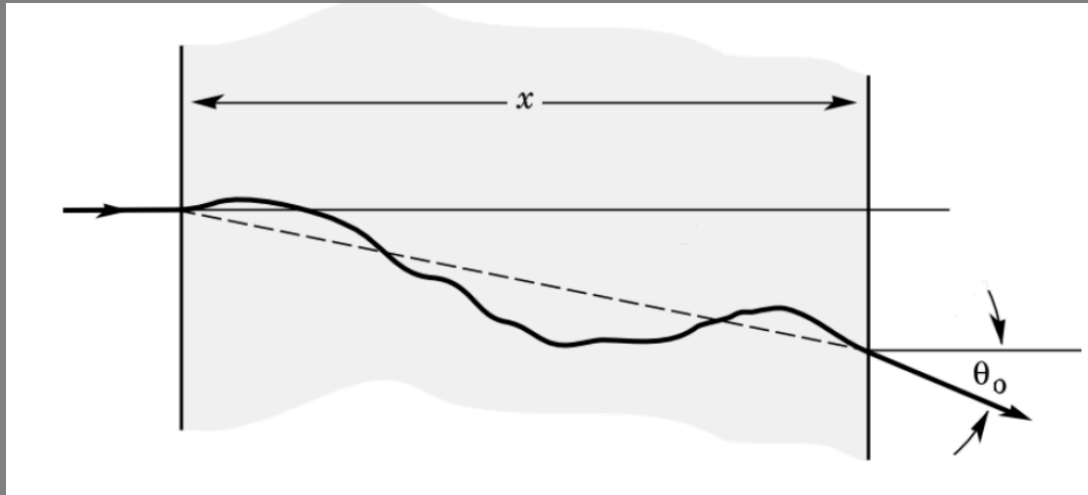


Figure 5: Value of $|B|$ (left) and field lines (right) predicted on a longitudinal section of the CMS detector, for the underground model at a central magnetic flux density of 3.8 T. Each field line represents a magnetic flux increment of 6 Wb.

Multiple coulomb scattering



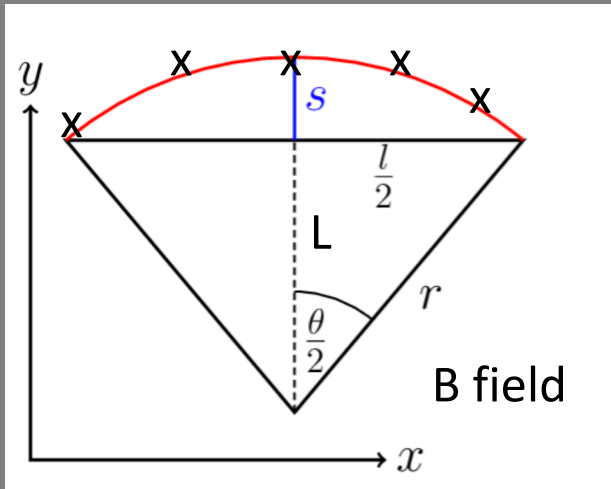
Like Rutherford scattering

$$\Theta_0 = \frac{0.0136}{\beta c p [\text{GeV}/c]} Z_1 \sqrt{\frac{x}{X_0}}$$

Characteristic width of Gaussian

Measure sagitta $s \rightarrow$ momentum resolution

- Recall $p = q r B \rightarrow p(\text{Gev}/c) = 0.3 R(\text{m}) B(\text{T})$



What is Δs ? The uncertainty on s ? σ_x / \sqrt{N}

Where N is the number of measurements along L .

$$L = r \theta$$

$$s = r(1 - \cos \frac{\theta}{2}) \sim r \frac{\theta^2}{8} = \frac{L^2}{8r}$$

$$r = \frac{L^2}{8s}$$

$$\Delta p = 0.3 B \Delta r = 0.3 \frac{B L^2}{8 s^2} \Delta s$$

$$\frac{\Delta p}{p} = \frac{\Delta s}{s} = \frac{\sigma_x}{\sqrt{N}} \frac{8 p}{L^2 q B (0.3)}$$

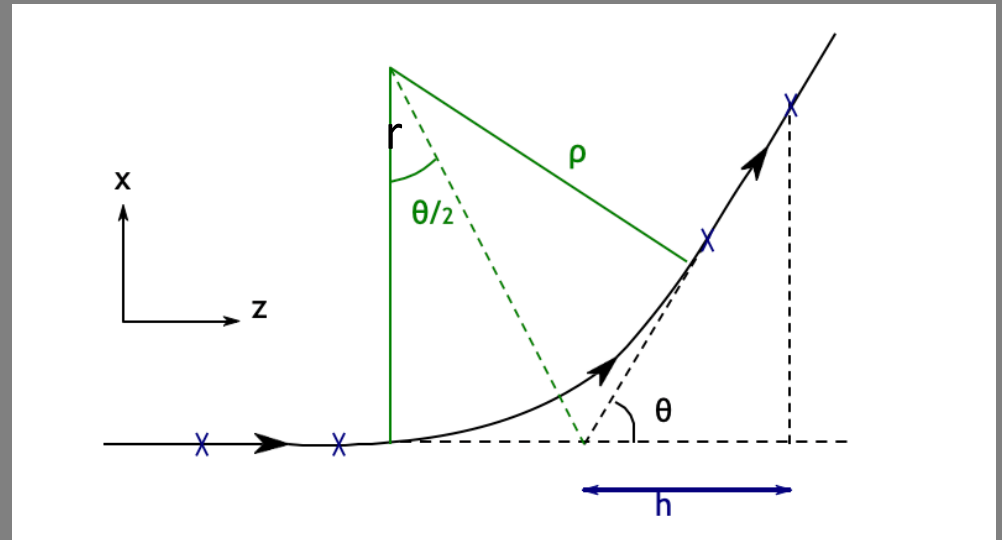
$$\Rightarrow \frac{\Delta p}{p} \sim p$$

Add multiple scattering to the resolution

Multiple scattering will change Θ a bit.

But $\Theta = L/r = 0.3 B L/p$

$$\Delta p/p = \Delta \Theta / \Theta = \Theta_0 / \Theta$$



$$\left(\frac{\Delta p}{p}\right)_{ms} = \frac{\Theta_0}{\Theta} \sim \frac{.04}{\beta L B} \sqrt{\frac{L}{\chi_0}}$$

χ_0 - radiation length

Independent of p !

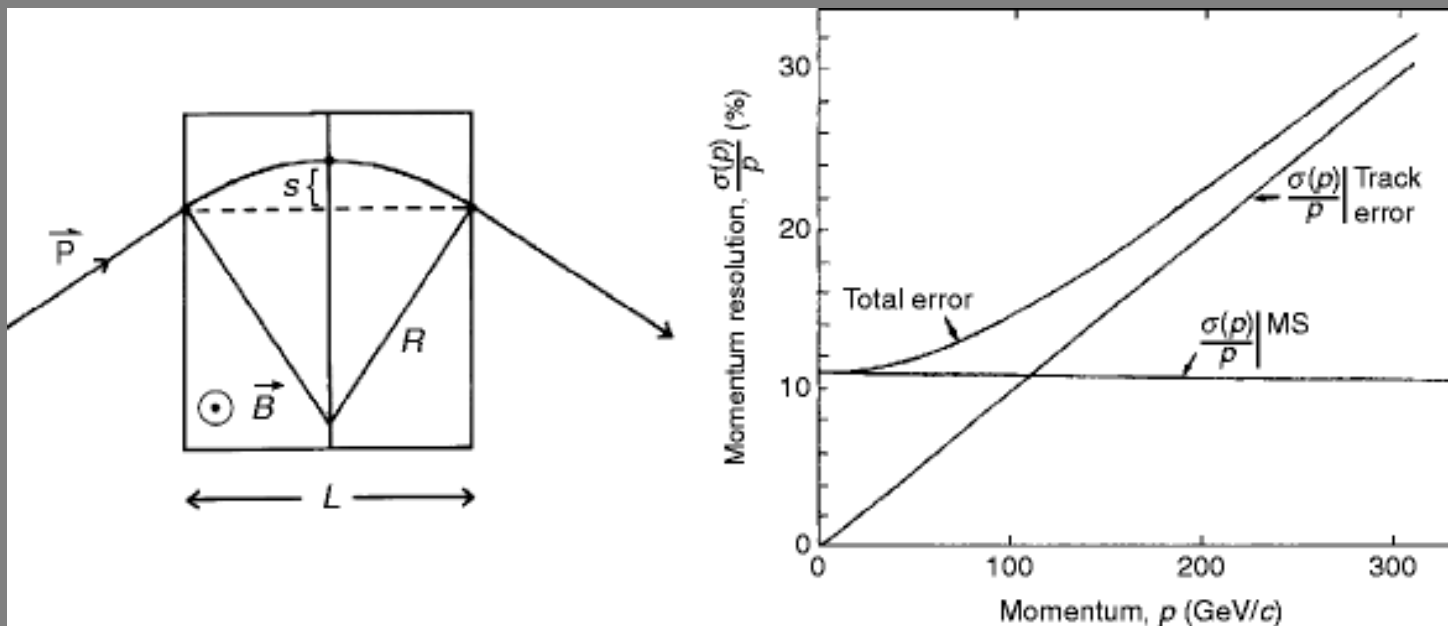
Momentum resolution

The contribution due to MS is constant with momentum!

And gives the limit for low p . The contribution from the position measurement

$$\left(\frac{\Delta p}{p}\right)_{\text{total}} = \sqrt{\left(\frac{\Delta p}{p}\right)_{\text{Sagitta}}^2 + \left(\frac{\Delta p}{p}\right)_{\text{MS}}^2}$$

multiple scattering

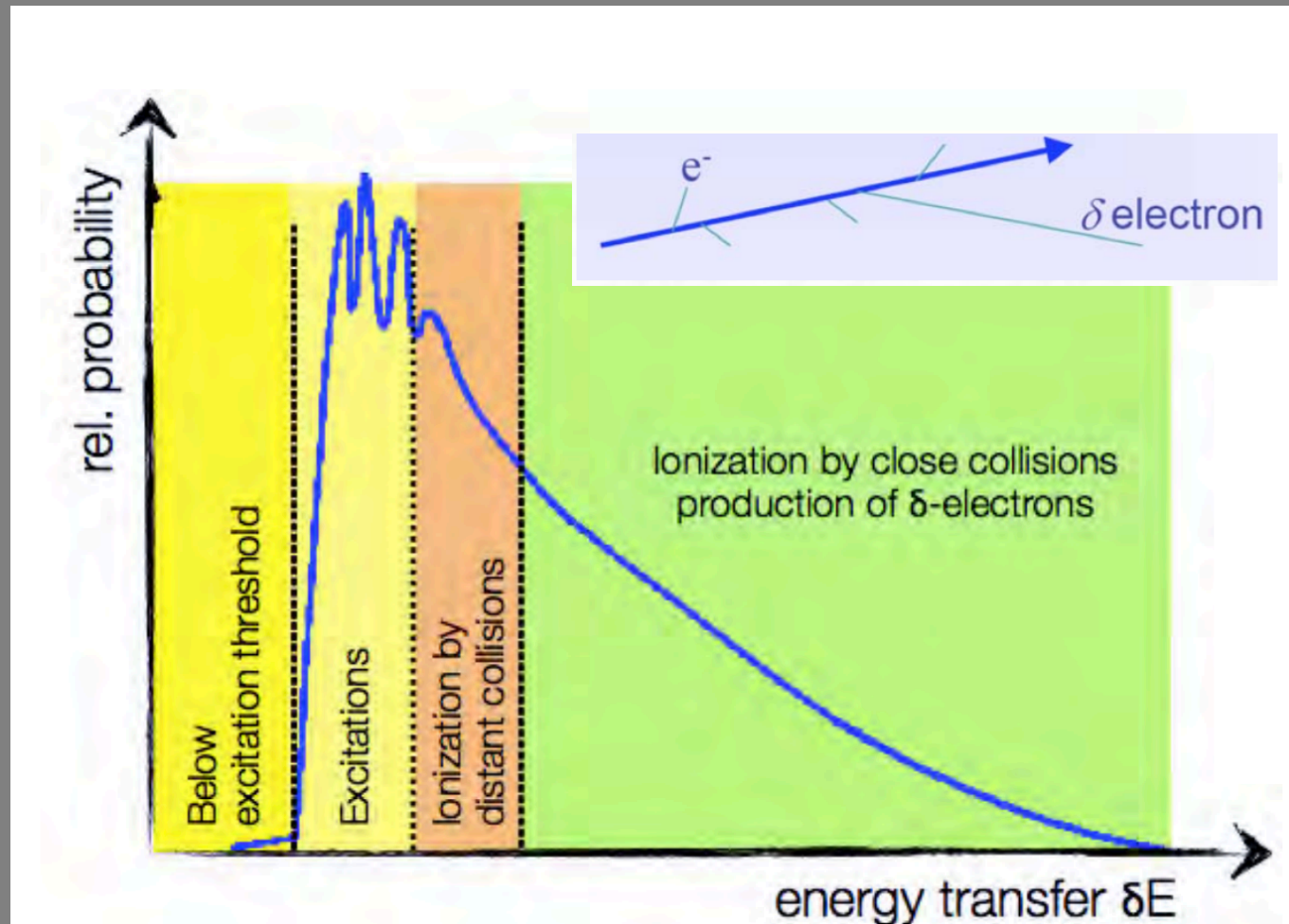


If you consider a 100 GeV muon -

Traversing 1m steel gives $\Theta_0 \sim 4$ mrad or 4mm over a meter

Traversing 1 m of air gives $\Theta_0 \sim 0.02$ mrad or 20 microns

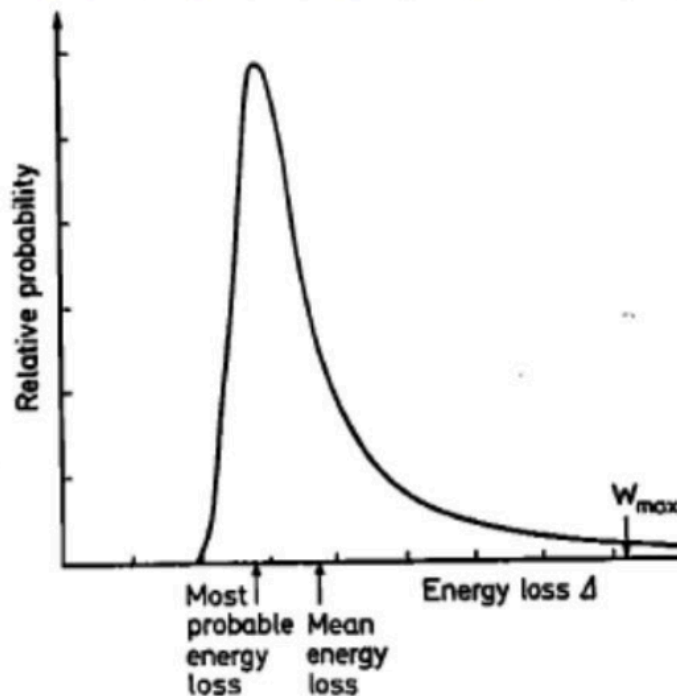
Energy loss fluctuations in material affect our measurements



Especially at low momentum

Energy loss distributions

B-B is average energy loss, there are fluctuations due to close collisions. Muon leaves minimum ionizing deposit in calorimeter



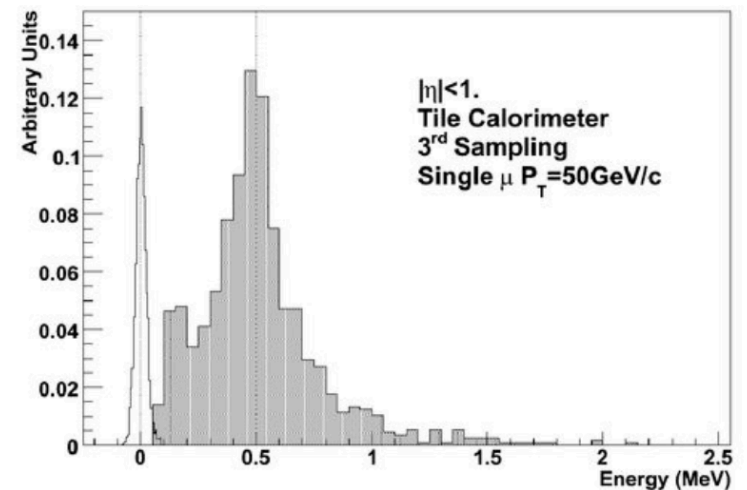
Noise

Mean = 0 MeV

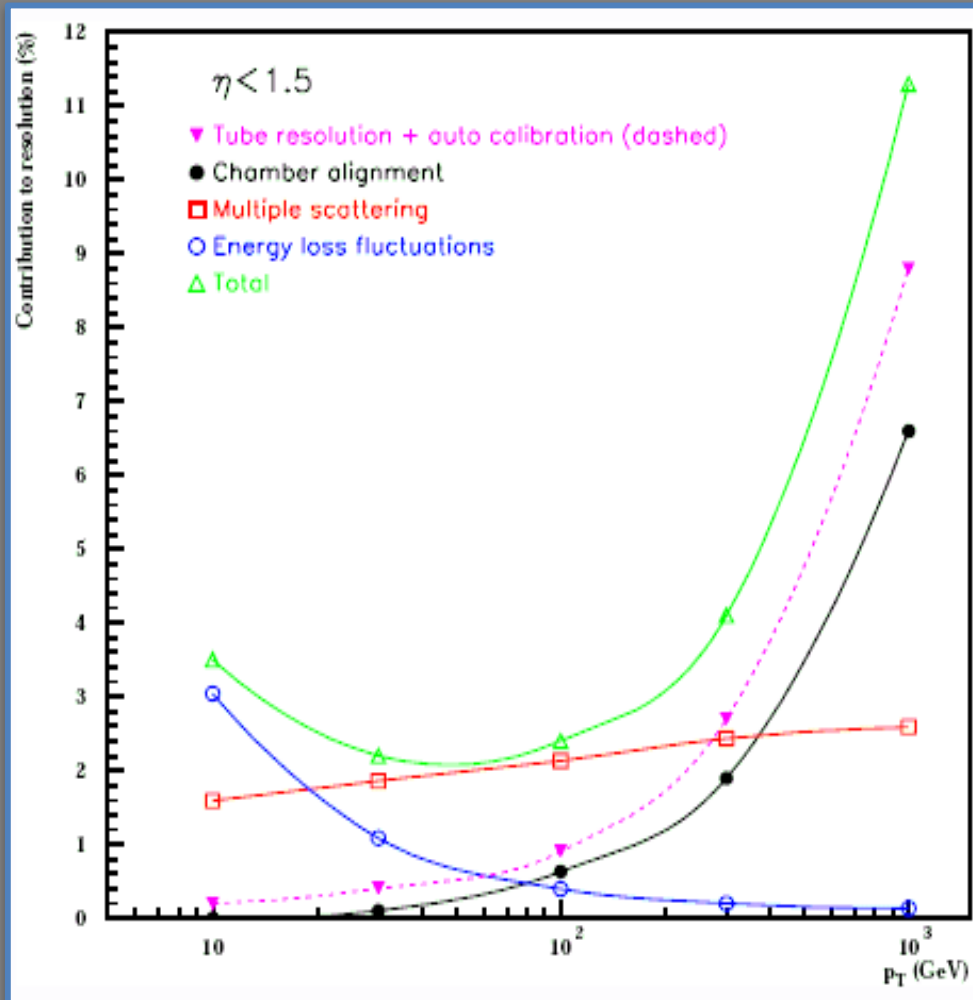
Sigma = 22 MeV

Signal

Mop \approx 500 MeV



Momentum resolution



ATLAS vs CMS Muon resolution

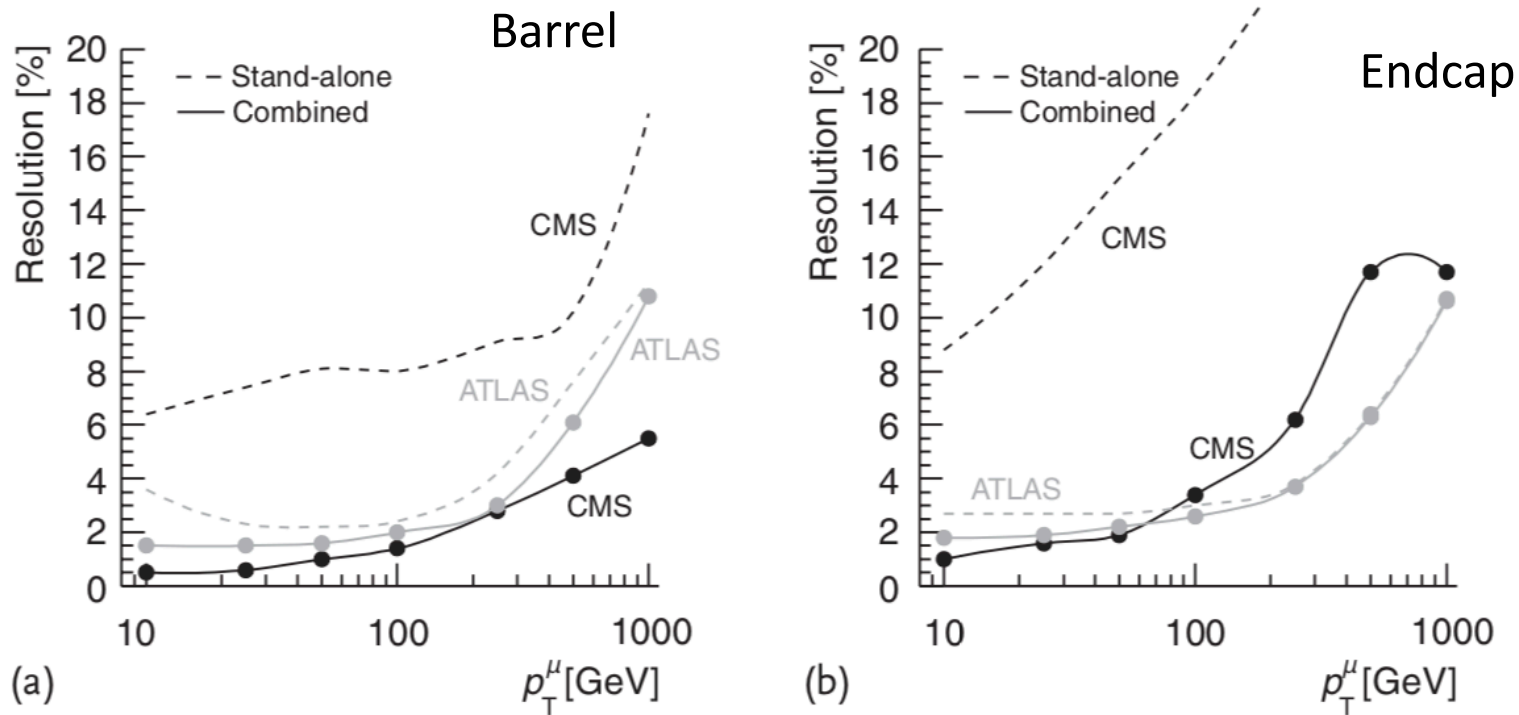


Figure 16.4 Momentum resolution of the ATLAS and CMS detectors after combining the momentum measurements of the inner

(a) momentum resolution for muons in the barrel region; (b) momentum resolution for muons in the endcap region.

Pion punch through

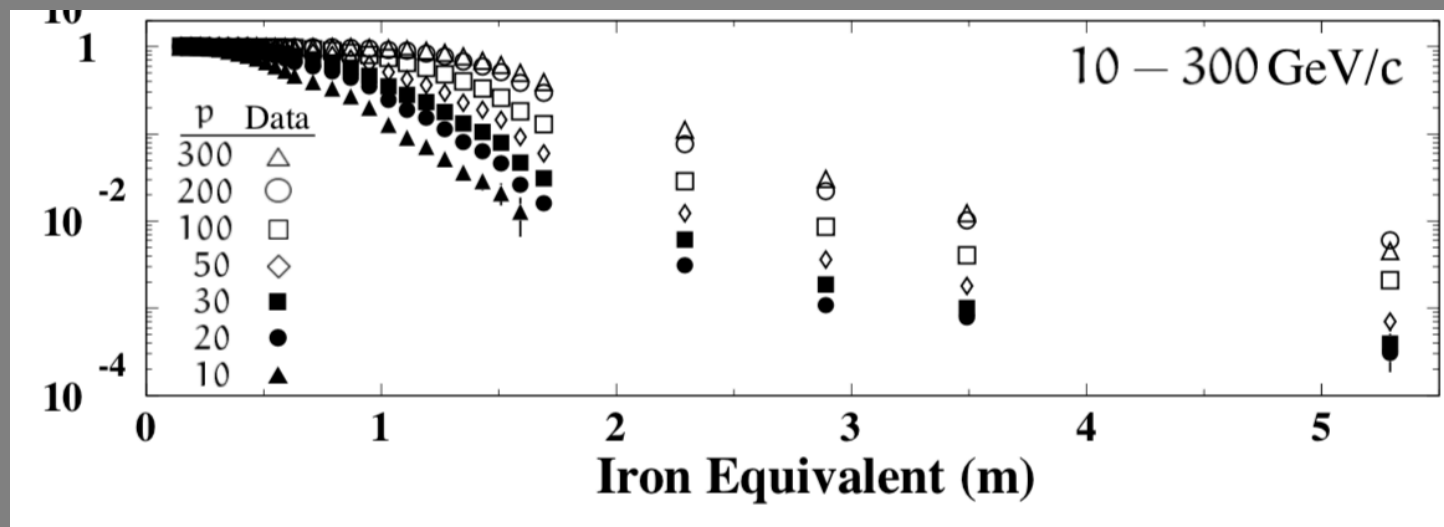
When does a pion look like a muon?

Pions



Iron

?



Pion Punchthrough probability - RD5

Why talk about resolution and punch through

We need to design the next pp experiment at the FCC

We can measure the track Sagitta in the inner detector

We can measure the bending of the track after the magnetic field coil.

We can measure the Sagitta in the instrumented return yoke

We can measure the muon independently after the calorimeter in a dedicated muon spectrometer with its own magnetic field

What should we do?

Why talk about resolution

It will help design the next experiment.



IP

Tracker

B

Calorimeter
& flux return

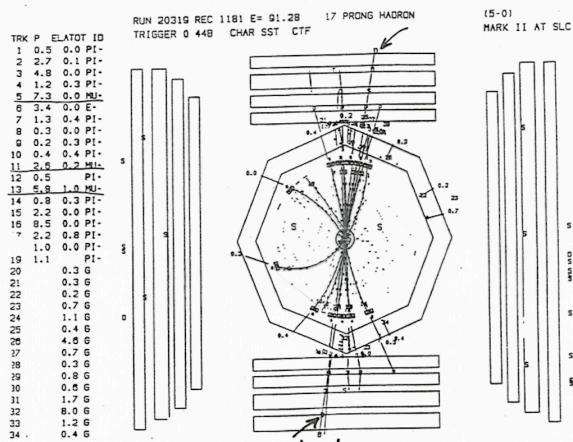
"B"

Muon

Use muon detector to tag muons

SPEAR

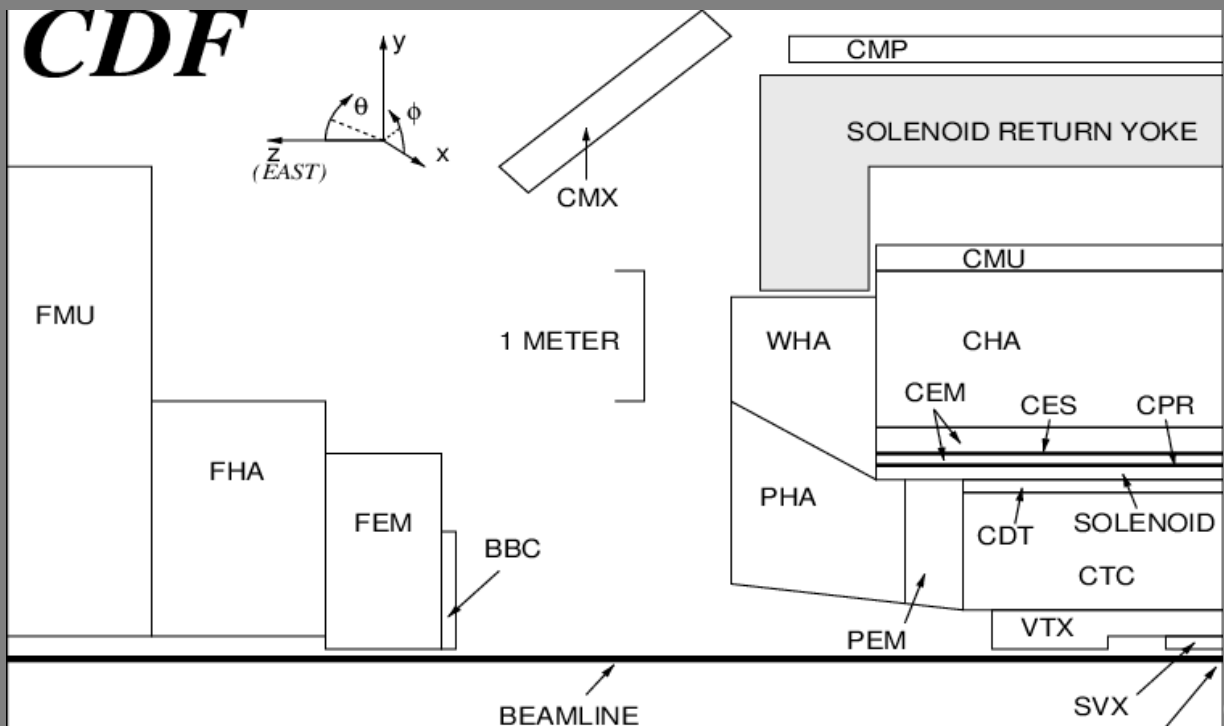
With 2 muons



MUON CANDIDATES:

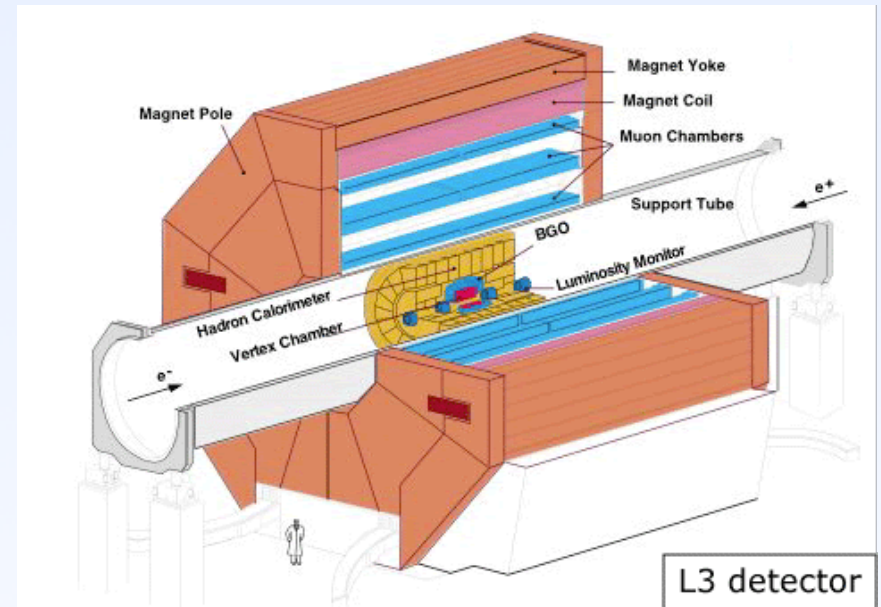
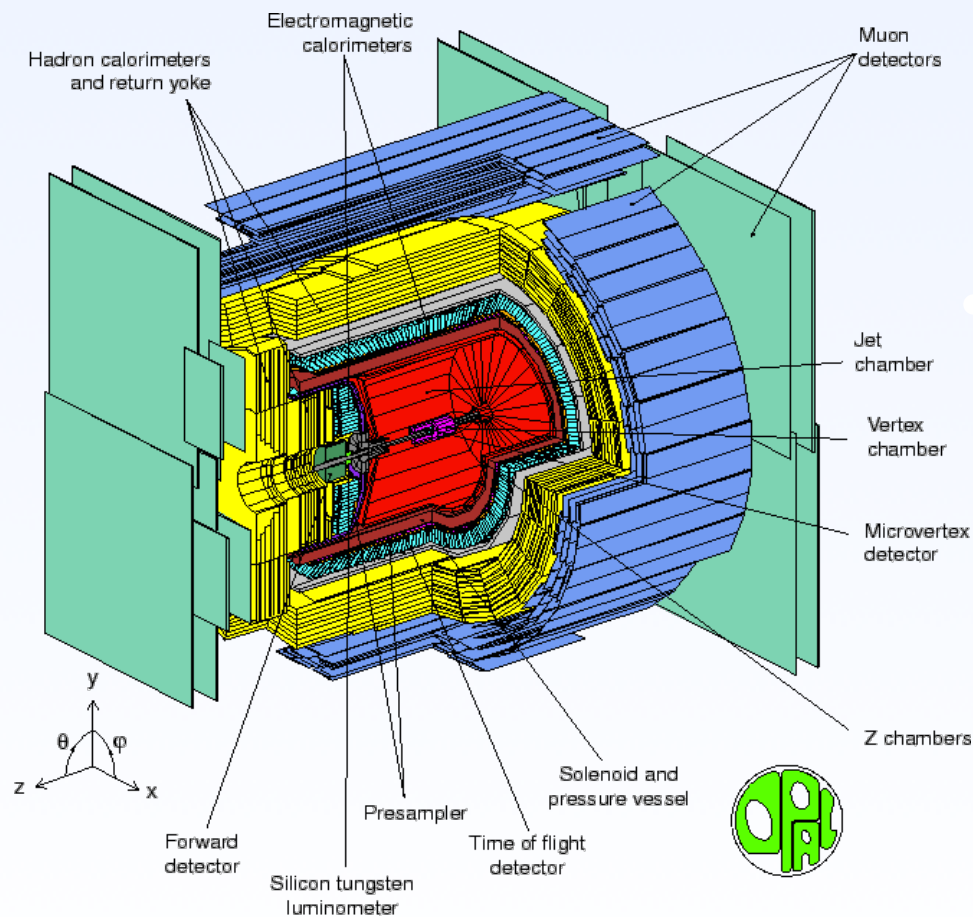
Track 5 $P = 7.3 \text{ GeV}/c$ $P_t = 0.8 \text{ GeV}/c$

Track 13 $P = 5.8 \text{ GeV}/c$ $P_t = 1.0 \text{ GeV}/c$

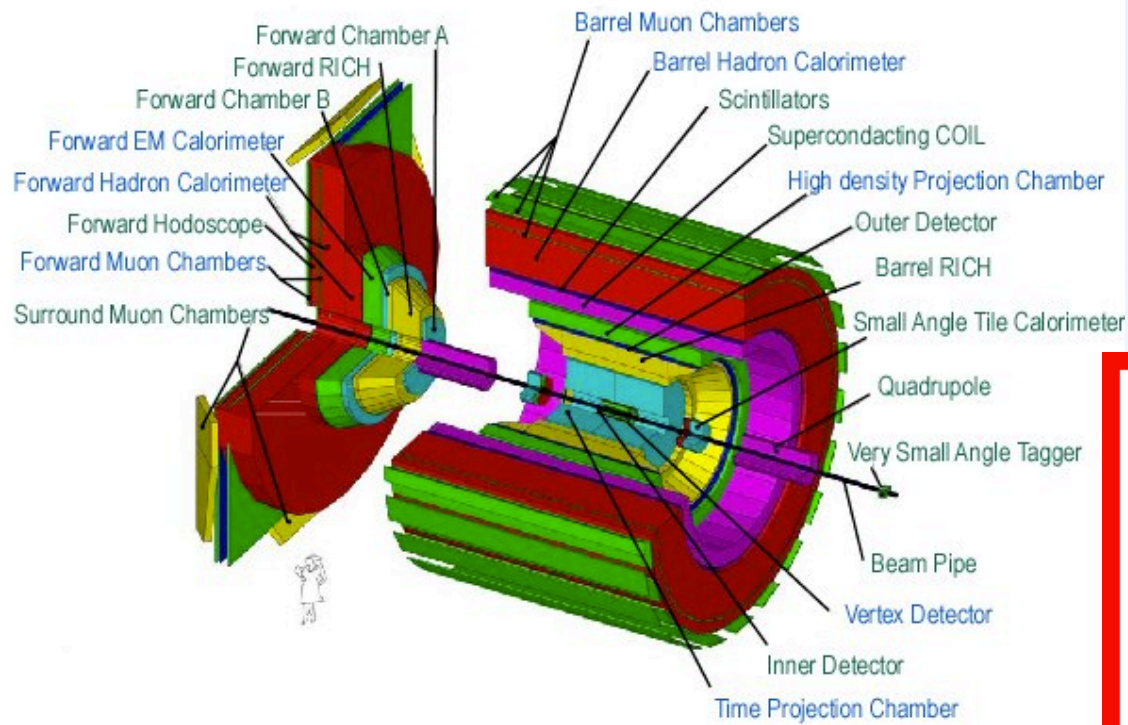


LEP experiments. e^+e^-

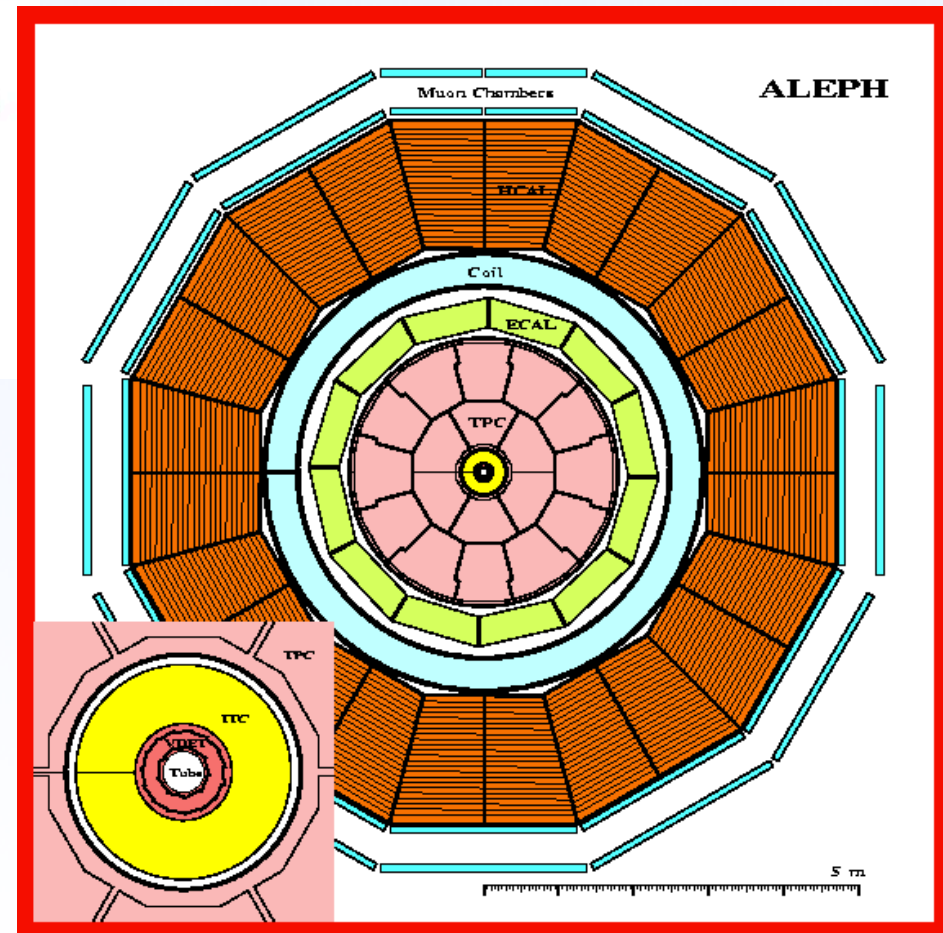
OPAL



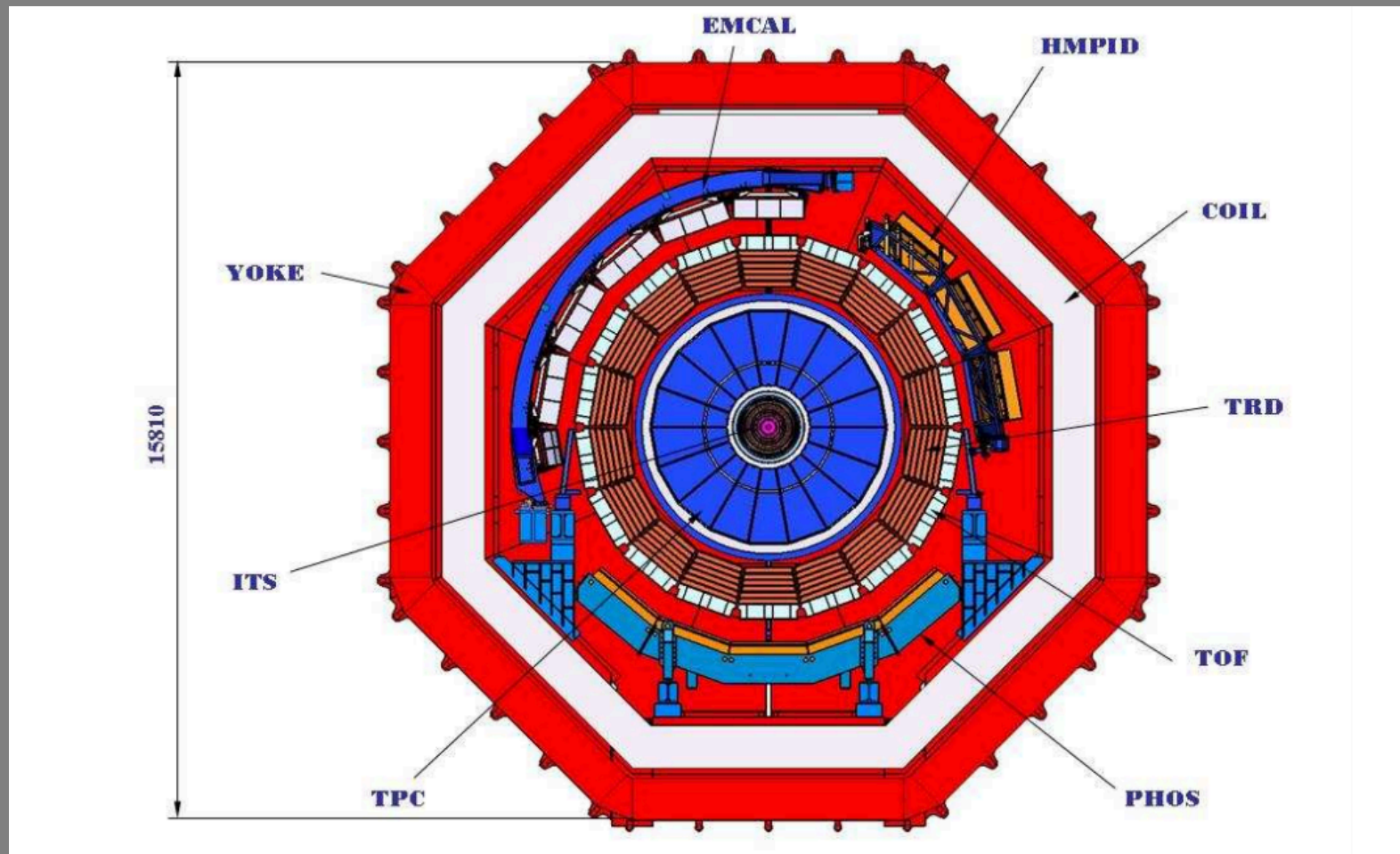
LEP detectors



Delphi

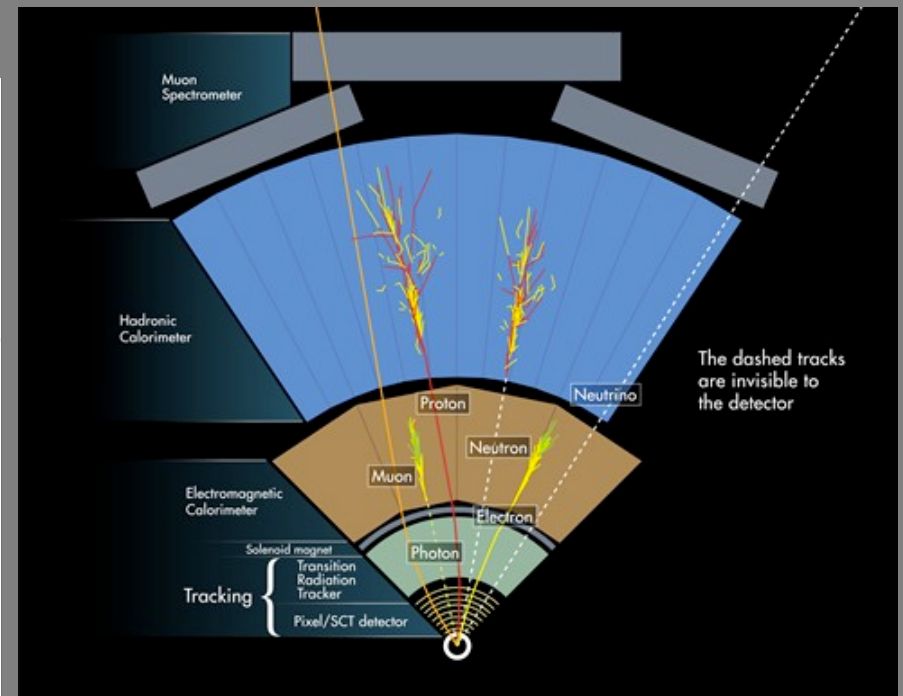
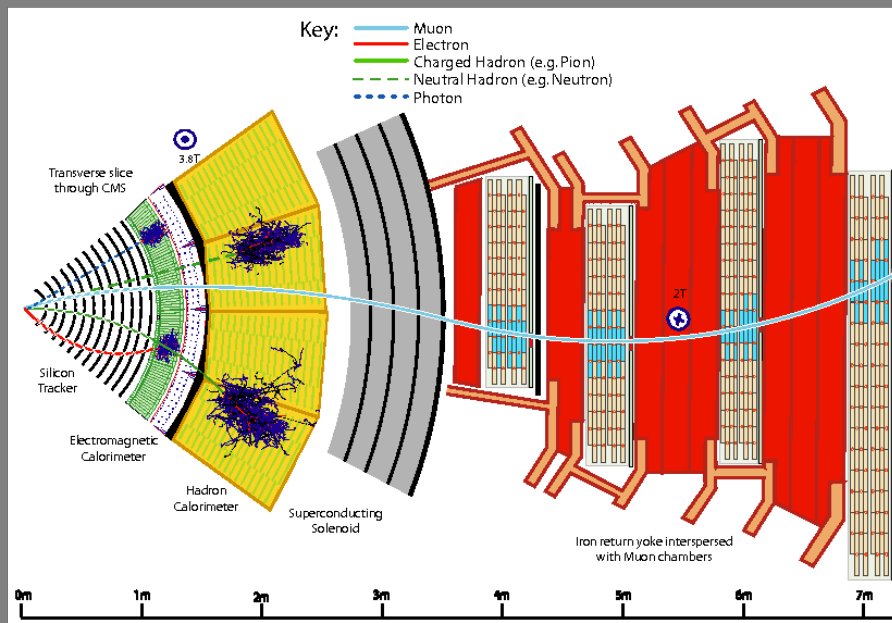


ALICE detector for heavy ion collisions



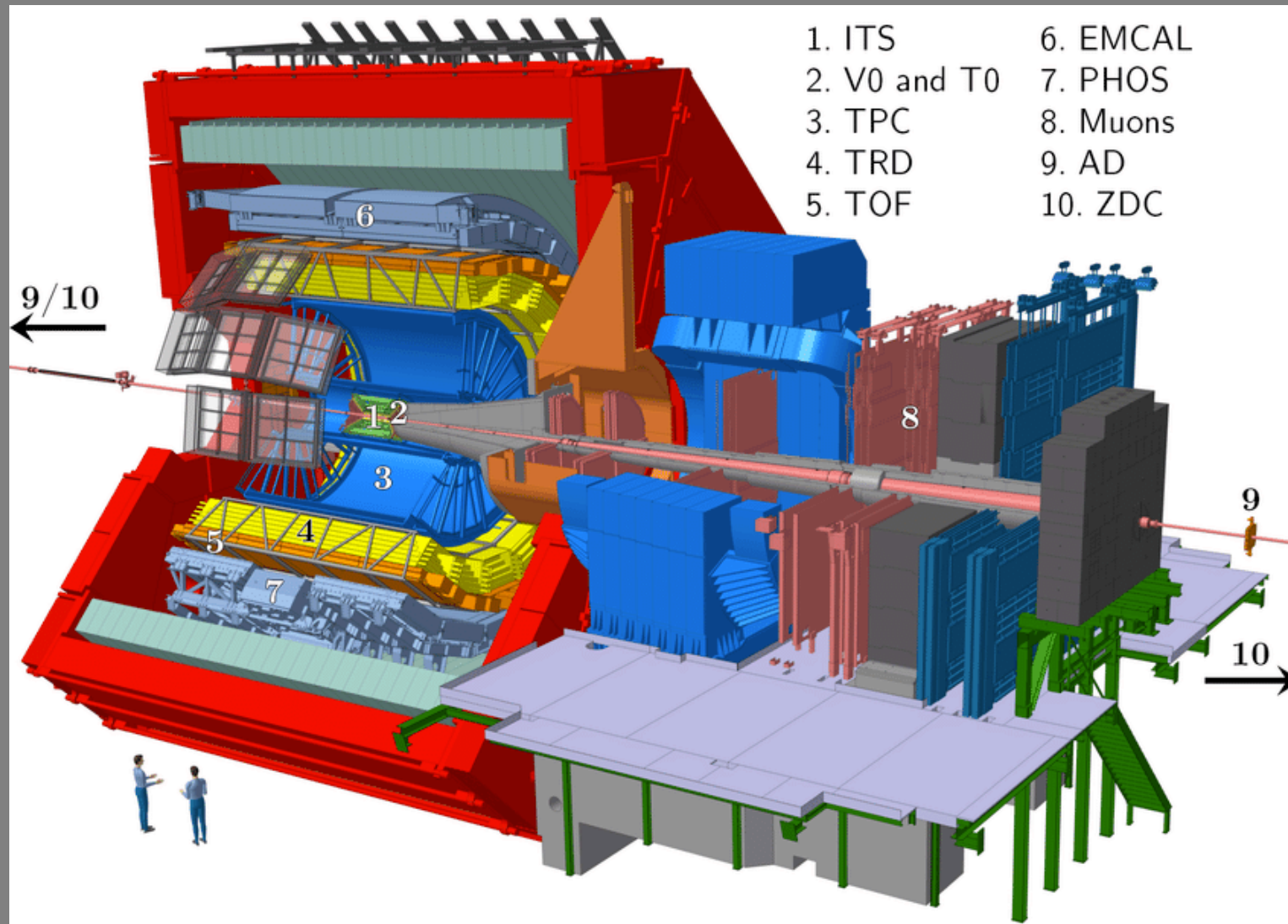
Central detector has no muon detection

- Need B fields precision detector, trigger.

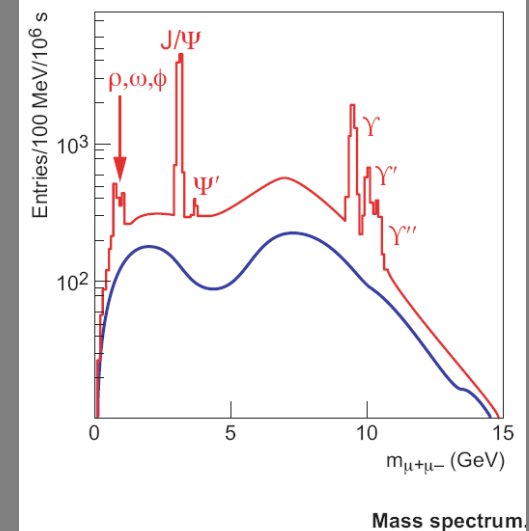
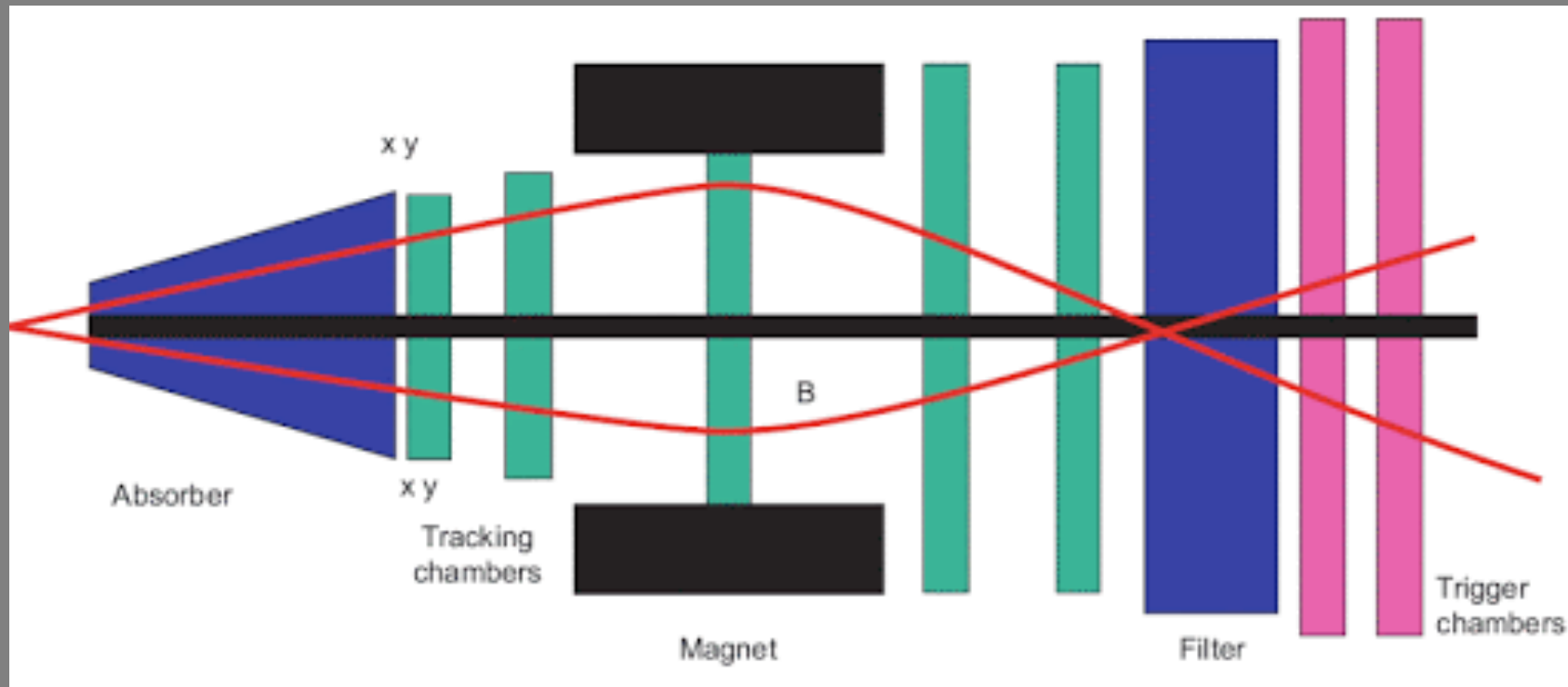


Both ATLAS and CMS have an inner detector immersed in a solenoidal field and a Muon spectrometer with a B field - return field of solenoid for CMS - Air core toroid for ATLAS
The combined resolution is best.

ALICE dedicated solid angle for muon detector

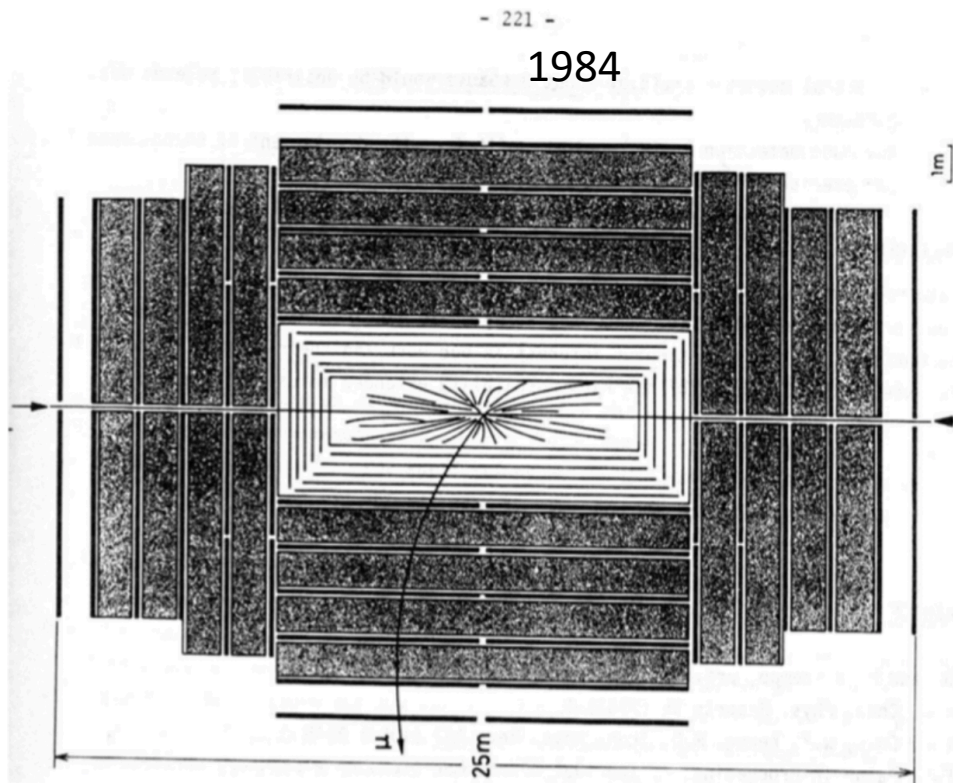


ALICE muon spectrometer - dipole magnet



First thoughts on an LHC detector

Detectors discussed at Lausanne

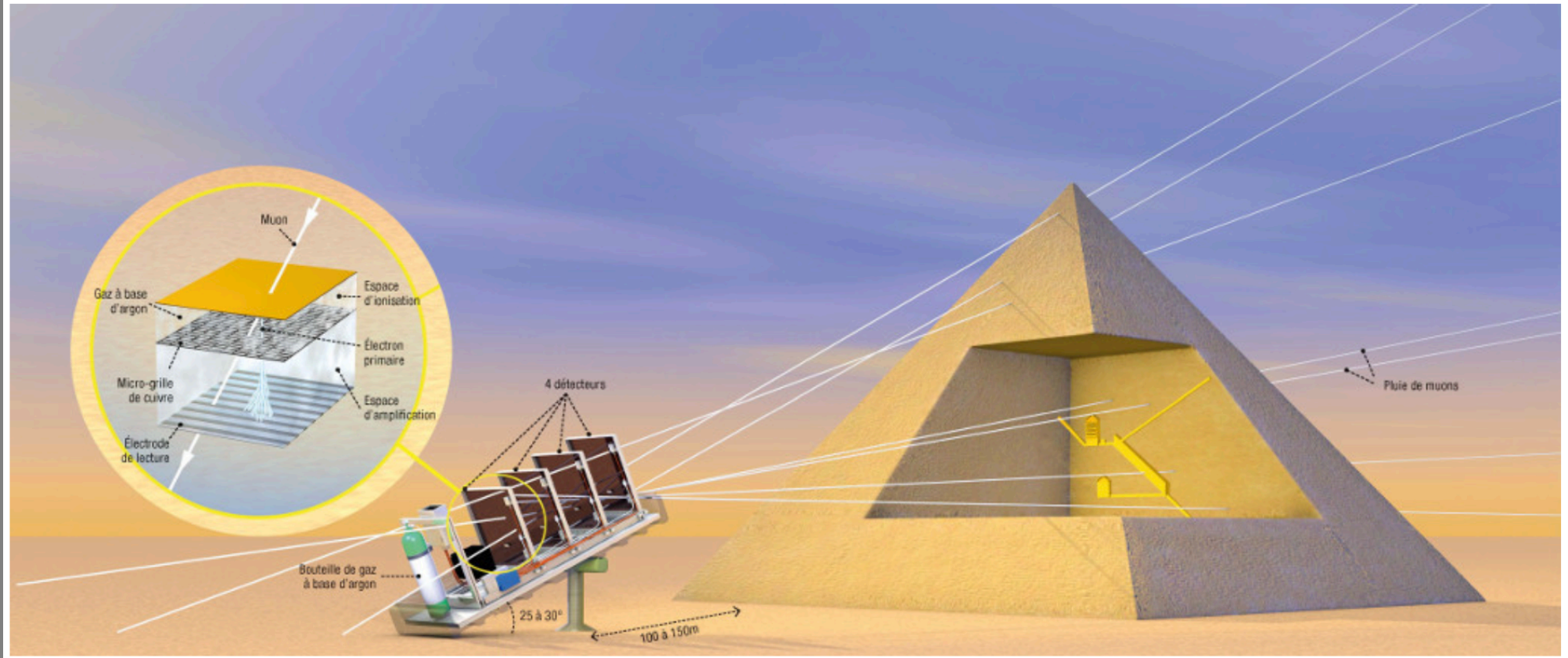


- Magnetized Iron ball
- Tracking a la « UA1 »

Look for missing matter

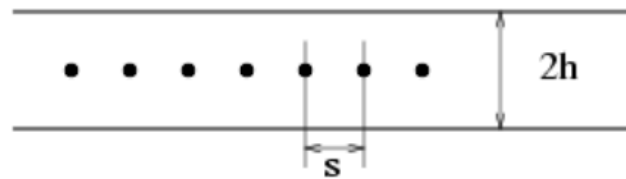
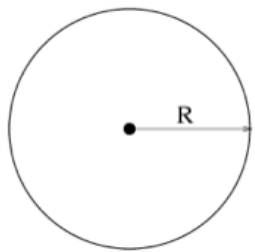
#ScanPyramids project

15 December 2016



With micromegas detectors! Tomorrow's lecture.

Tomorrow: Muon detectors I have known and weird problems they have had and New detector technologies.



This is what we have now - drift tubes, RPC's, CSC's, TGC's
What's next?